

WAM™ Arm

Inertial Specifications



Barrett Technology® Inc.

Inertial Data for the WAM arm.

This document presents the inertial data for the WAM robotic arm (both the 4- and 7-dof version) in support of computed-torque control techniques. This draft document is a work in progress and not ready to be released for general use. Critical feedback is encouraged.

Relevance and Approximation of “Reflected Inertia.”

Except for (generally impractical) direct-drive robotic arms, all multi-serial-link robotic arms have drive inertias whose main effect may be approximated as “reflected” inertias. Reflected inertias are only approximations because of the assumption that there is no cross-product interaction between the spinning drive components and the (generally rotating) frames in which they are embedded. Reflected inertias are amplified by the square of the drive-reduction-ratios which generally range from 30 – 1,000 for practical robotic arms, so the reflected inertias generally range from 1,000 – 1,000,000, easily contributing most of the inertia of a robot. It is interesting to note that most text books on robotics deemphasize or dismiss the contributions of reflected inertias even though they generally overwhelm the inertias of the moving links. The WAM is unique in that its ratios were selected to balance the two inertia sources for optimal backdrivability and so both inertia sources are important.

Relevance and Treatment of “Differential” Mechanisms.

Also, many, if not most, robotic arms minimize moving inertia through the use of drive mechanisms called “differentials” which allow a pair of motors to be placed on one side of two perpendicular, intersecting axes, such as at shoulders and wrists, thereby minimizing the moving inertia of those motors. However, differentials also require special treatment when applying the approximation of “reflected” inertias because of the 2x2 motor-joint couplings, especially in the case of a high-backdrivability robot like the WAM. The couplings are given by the middle 2x2 transformations of Equation 1 for the shoulder, where $n_3 = 1.6800$, and Equation 2 for the wrist, where $n_6 = 1.0000$. For any pair of computed Joint torques the kinematically equivalent Motor torques are easily calculated as the sum of 2 polynomials with constant coefficients.

$$\begin{pmatrix} M\tau_1 \\ M\tau_2 \\ M\tau_3 \\ M\tau_4 \end{pmatrix} = \begin{pmatrix} \frac{-1}{N_1} & 0 & 0 & 0 \\ 0 & \frac{1}{2N_2} & \frac{-n_3}{2N_2} & 0 \\ 0 & \frac{-1}{2N_2} & \frac{-n_3}{2N_2} & 0 \\ 0 & 0 & 0 & \frac{-1}{N_4} \end{pmatrix} \begin{pmatrix} J\tau_1 \\ J\tau_2 \\ J\tau_3 \\ J\tau_4 \end{pmatrix}$$

Equation 1: Arm Joint-to-Motor torque transformations

$$\begin{pmatrix} M\tau_5 \\ M\tau_6 \\ M\tau_7 \end{pmatrix} = \begin{pmatrix} \frac{1}{2N_5} & \frac{-n_6}{2N_5} & 0 \\ \frac{1}{2N_5} & \frac{n_6}{2N_5} & 0 \\ 0 & 0 & \frac{-1}{N_7} \end{pmatrix} \begin{pmatrix} J\tau_5 \\ J\tau_6 \\ J\tau_7 \end{pmatrix}$$

Equation 2 - Wrist Joint-to-Motor torque transformations

The inertial data are calculated and employed separately for Frames and Drives:

1. Link (or Frame) inertias that are associated by Coordinate Frame number (0-7).
2. Drive inertias that are associated by Motor number (1-7).

How to Use the Inertia Data

Generally, motor torques are calculated in the following sequence:

1. Use the Frame inertias in the generalized robot equation. Apply either LaGrange or numerical Newton-Euler methods to translate desired robot forces and torques described in world Cartesian coordinates into equivalent, computed, joint torques.
2. For axes driven by differentials at the shoulder and wrist, apply the 2x2 torque transformations to translate the computed joint torques into the kinematically equivalent ideal motor torques.
3. For each ideal motor torque, calculate an adjusted motor torque required to provide the appropriate additional motor-output torque that overcomes the drive inertias.

Frame Inertias (and Related Mass Data)

See the data in Table 2 through Table 11 that correspond to the model graphics in Figure 4 through Figure 13. Some of the data in the tables is not necessary for most computed-torque calculations. All units are in kilograms and meters unless otherwise indicated. Generally, 13 values are important:

- Mass.
- X, Y, Z location of the Center of Mass.
- Ixx through Izz (9 inertia-tensor values).

Drive Inertias

The motor-drive inertias are reported in Table 1. The data is derived from model geometries shown in Figure 14 through Figure 24. In these models, roller and ball bearings are generally separated into their stationary and moving components. The geometric information from these models is summarized in Table 23 along with the associated cable diameters and resulting intermediate and total drive ratios. The inertial data from these models, in which only one inertia tensor (bolded and underlined) value is relevant are given in Table 12 through Table 22. The additional inertia data can, for example, quantify corrections in the “reflected”-inertia assumptions though it is believed that these errors are well under 1%. Table 24 calculates the lumped pinion+cable inertia for each drive body and gives its equivalent inertia at the rotor end of the drive. Table 25 then combines the various drive-components for each motor-drive number.

Table 1 -- Drive Inertias for all WAM DOFs.

Motor Drive Number	Total Drive Inertia at Rotor (kg-m ²)	Drive Ratios	Total Reflected Inertia at Output (kg-m ²)
M1	0.00011631	42.00	0.205190
M2	0.00011831	28.25	0.094428
M3	0.00011831	28.25	0.094428
M4	0.00010686	18.00	0.034628
M5	0.00001685	9.48	0.001584
M6	0.00001745	9.48	0.001641
M7	0.00000142	14.93	0.000318

There are several one-page graphics that show an assembly (rigid body) with its associated coordinate frame and reports of mass parameters (mass, CG, and inertia tensor). Many of the components of the assembly are rendered as transparent to make clear what components are and are not included in the assembly. The numerical data is reported with the screen-shot graphic (to prevent any possibility of associating data to the wrong model). However the data is then repeated as text on the page following each graphic to allow easy copy-and-paste to a user's program.

Figure 1 shows the relationships between pulleys throughout the WAM. The present-day WAM has changed little since this artist's sketch was produced in 1987. In modern WAMs there are twin cables in each 2nd stage where the illustration shows only one cable, and the base motor has flipped orientation for better compactness. Figure 2 helps clarify the operation of the differential. It should be noted that the rotations of both differential-input pulleys are totally independent of the structure that supports them and (therefore) independent of the orientation of motor 4. One depends on the rotation of the M2 rotor and the other on the M3 rotor.

Figure 14 through Figure 16 are rigid-models required to calculate the “reflected” inertia of each of the 1st four DOFs of the WAM. In cases where there are sets of ball or roller bearings supporting a spinning body, we deleted ½ of the bearings as an approximation. For the elbow pulley-pinion, we can take an average of the case with all bearings installed (Figure 17) and the case of no bearings installed.

Cable, pinion, and pulley diameter/radius geometric data given in Table 23 enable calculation of all transmission ratios including intermediate ratios required to associate the “grenades” of Figure 15 and elbow-pulley-pinion set of Figure 17 with their associated joint inertias. The only ratio not given in this table (but given in this sentence) is the 1.68:1 ratio between the differential-input-pulley radii and the output pulley radius for calculating the J3 reflected inertias.

The (unreflected) motor rotor inertia (I_{zz} only) of Figure 14 is identical for each motor of the 1st four DOFs of the WAM = 0.00010569 kg-m². Also for all 4 DOFs, this rotor drives a pair of identical Stage-1 cables (Sava Cable Part Number SN2047 in Table 23) that have a mass of 0.013 kg each, or 0.026 kg total. The radius to the centerline of these cables where they are wrapped onto the scalloped pinion of the rotor is 0.009 m (9 mm), and since the entire length of cable translates as the same velocity one can lump the both cable masses at the 9-mm radius. In this case the inertia of the cables is $(0.026 \text{ kg}) \cdot (0.009 \text{ m})^2 = 0.00000178 \text{ kg-m}^2$, adding <2% to the rotor inertia. The combined inertia is then = 0.00010747 kg-m².

At least for the 1st three WAM motor drives, the 1st and 2nd stages are coupled through a pair of “grenades” (Figure 15) that have an 11-mm radius pinion at one end driven by a stage-1 cable and a 33-mm-radius pulley at the other that drives a pair of stage-2 cables.

Cautions:

While the robot inertias are given here, several modeling errors are known to exist:

1. Machining, plastics, and composite-layup tolerances, especially important with thin (WAM) structures.
2. Ceramic, anodize/Teflon-surface-coating densities not accounted for.
3. Density variances from (allowed) tolerances in alloy contents, plastics, ceramics, and composites.
4. Inability to model (especially stranded) wires and cables in any practical manner, especially their paths as they flex.
5. Lack of knowledge of the proprietary assembly of components, such as bearings, wires, electrical cable assemblies, connectors, etc.
6. Treating ball and roller bearings as if they had only an inner and an outer race, when, in fact the balls themselves belong to neither, have individual (unmodelled) spins, and their CGs travel neither with the inner race nor the outer race. Ball retainers also move at the average ball velocity and not with either race.
7. Ball bearings in the WAM model are modeled as single parts, not as assemblies of races, balls, retainers, shields, and lubricants.
8. Modeling most threaded holes as if only the tap drill (but not the tap) has been applied.
9. Adhesives not modeled.
10. Lubricants not modeled and not clear how to associate velocities.

Background

Historical analysis of robotic arms (Paul, Craig, Spong, etc.) assumes a set of kinematically linked rigid bodies that can be assigned coordinate frames consistent with DH parameters. The analysis holds strictly only for direct-drive robots in which the rotor is integral with one rigid body and the stator is integral with an adjacent rigid body.

While direct-drive motors have outstanding inherent backdrivability with unity transmission ratios ($N=1$) they are far too massive and power-inefficient for the joint-torque demands of practical robots. So virtually all conventional robots use geared speed reducers in the form of harmonic drives with transmission ratios of $40 < N < 400$ to match the power capability (which varies as N^2) of practical motors with the speed and torque requirements of robotic arms. DH-kinematic analysis is not equipped to account for the spinning motor rotors, which impart significant momentum effects because of the amplified speeds involved.

It has been long proposed to treat the fast-spinning backdriven motor-rotor inertias as “reflected” inertias. However, it should be said that, while the “robot math” used to calculate computed

torques is precise for a direct-drive robot, even the precise calculation of reflected inertias does not and cannot account for some inertial interactions between fast spinning rotors and the velocities of the motor bodies containing those rotors. We are not aware of published analyses that have explored these errors.

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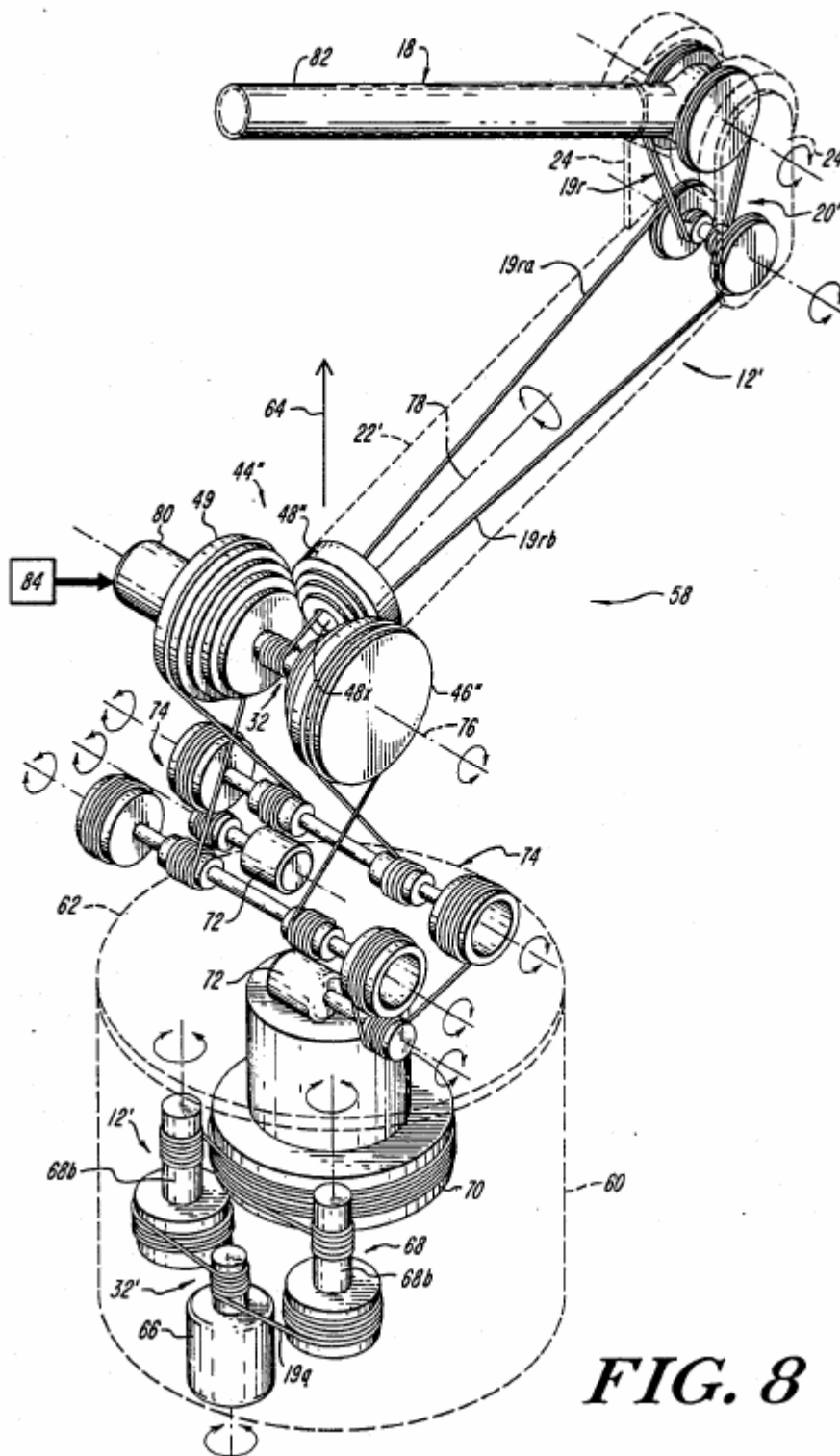
**FIG. 8**

Figure 1 -- Artist's sketch of WAM cable drives.

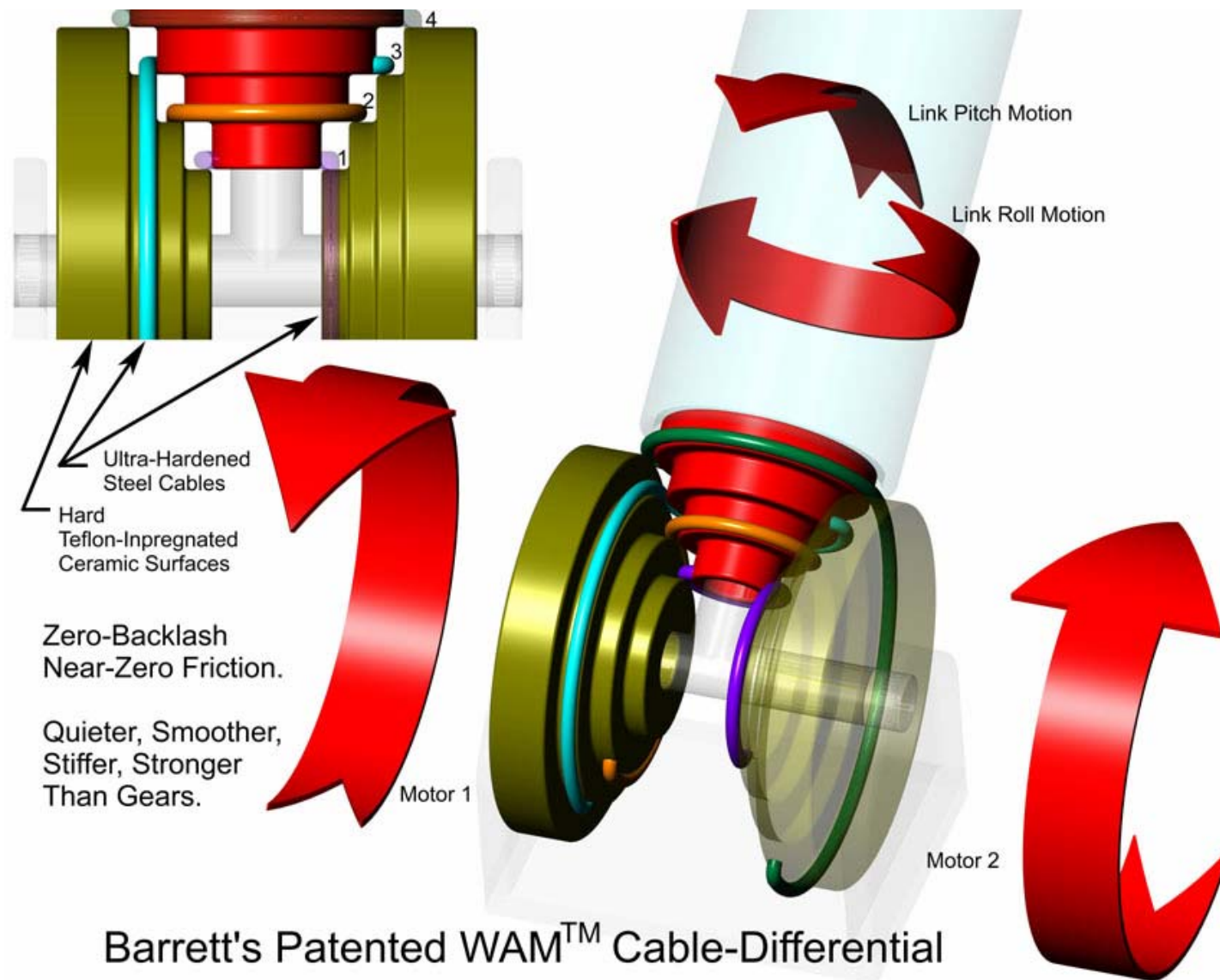


Figure 2 – Basic operation of the cabled differential mechanism used in the WAM shoulder. The WAM wrist differential operates similarly.

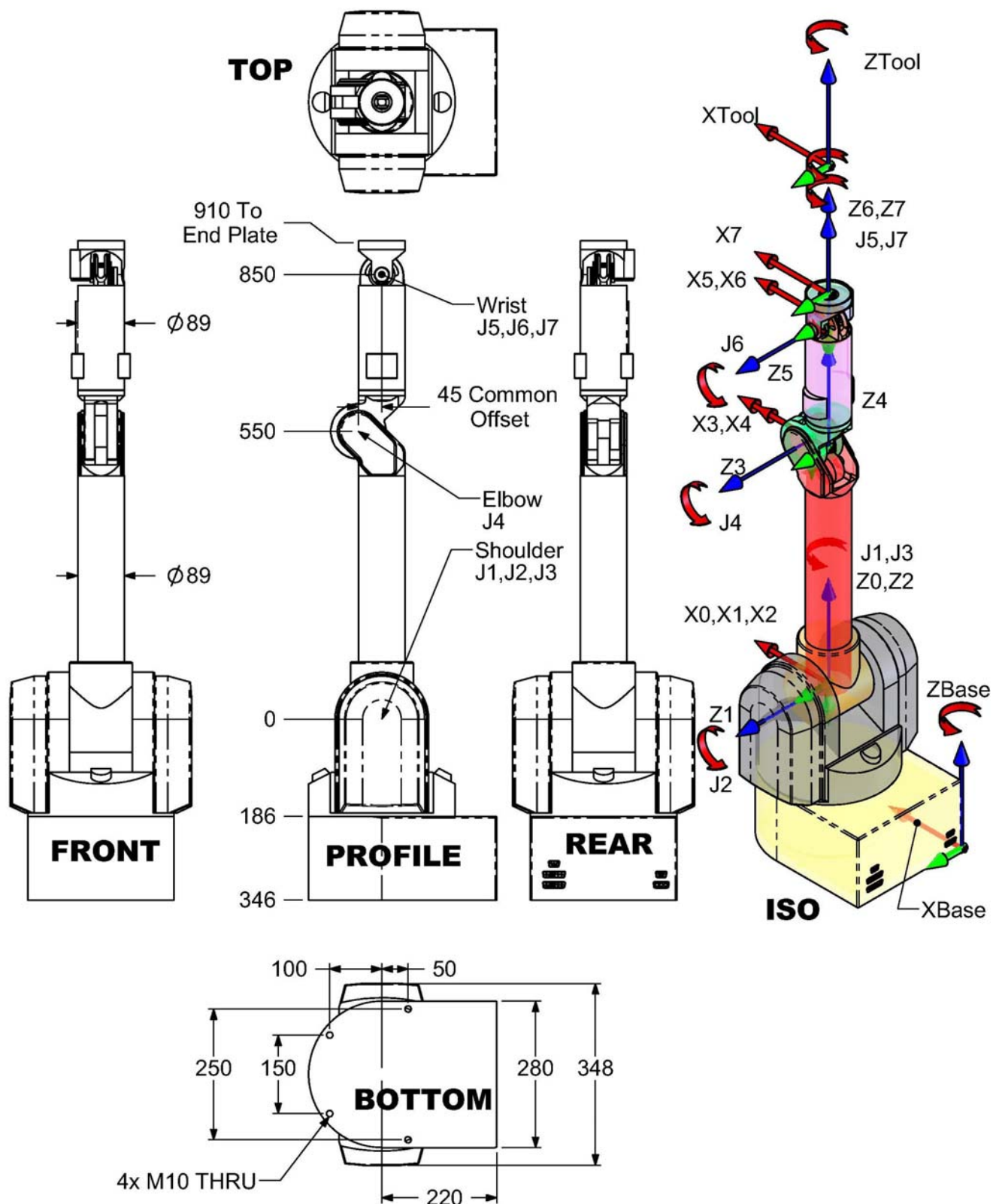


Figure 3 -- WAM Coordinate Frames.

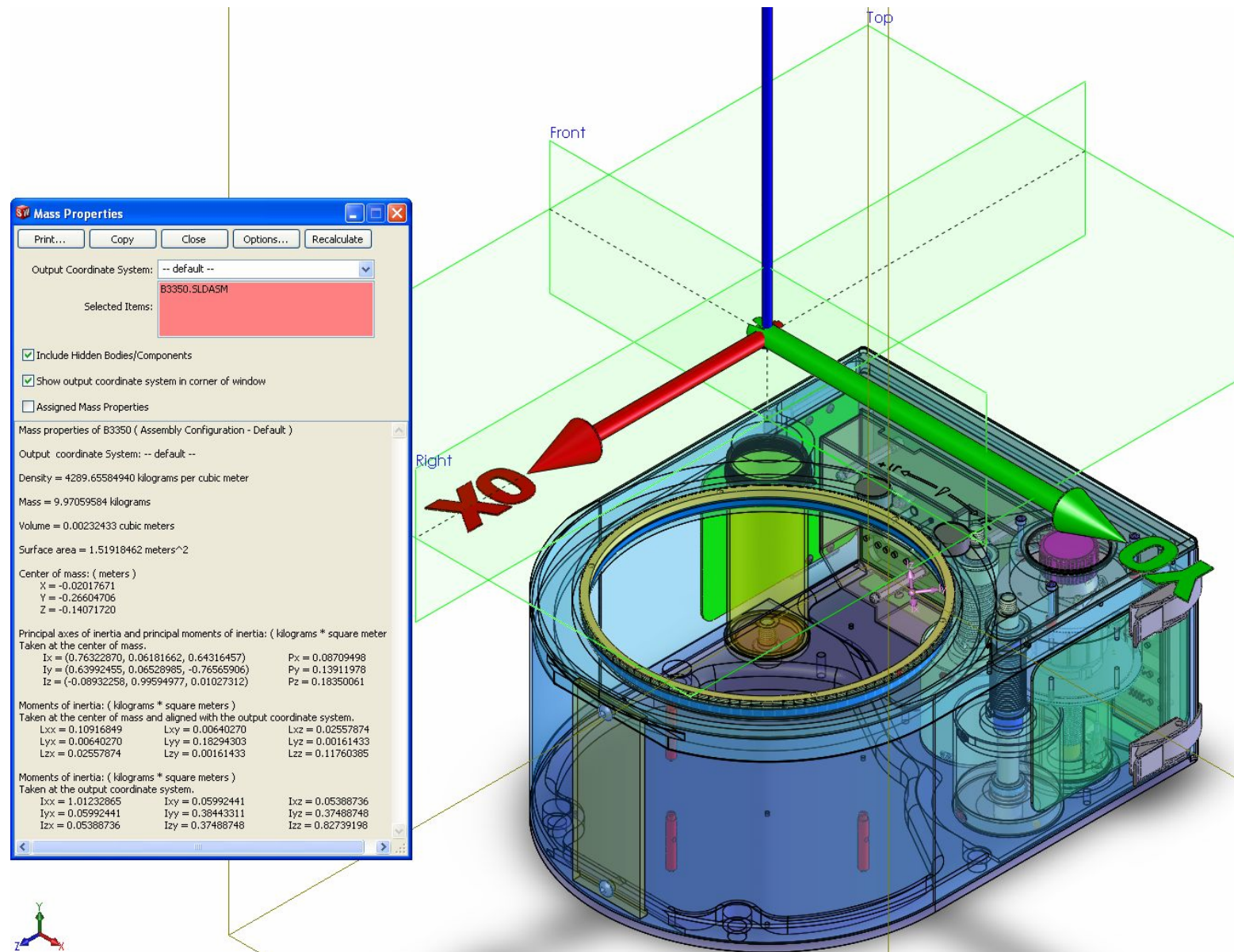


Figure 4 -- Frame 0 Inertia

Table 2 --Frame-0 Mass properties of B3350 (Assembly Configuration - Default)

Density = 4289.65584940 kilograms per cubic meter

Mass = 9.97059584 kilograms

Volume = 0.00232433 cubic meters

Surface area = 1.51918462 meters²

Center of mass: (meters)

X = -0.02017671

Y = -0.26604706

Z = -0.14071720

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.76322870, 0.06181662, 0.64316457)$ $P_x = 0.08709498$

$I_y = (0.63992455, 0.06528985, -0.76565906)$ $P_y = 0.13911978$

$I_z = (-0.08932258, 0.99594977, 0.01027312)$ $P_z = 0.18350061$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.10916849$ $L_{xy} = 0.00640270$ $L_{xz} = 0.02557874$

$L_{yx} = 0.00640270$ $L_{yy} = 0.18294303$ $L_{yz} = 0.00161433$

$L_{zx} = 0.02557874$ $L_{zy} = 0.00161433$ $L_{zz} = 0.11760385$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 1.01232865$ $I_{xy} = 0.05992441$ $I_{xz} = 0.05388736$

$I_{yx} = 0.05992441$ $I_{yy} = 0.38443311$ $I_{yz} = 0.37488748$

$I_{zx} = 0.05388736$ $I_{zy} = 0.37488748$ $I_{zz} = 0.82739198$

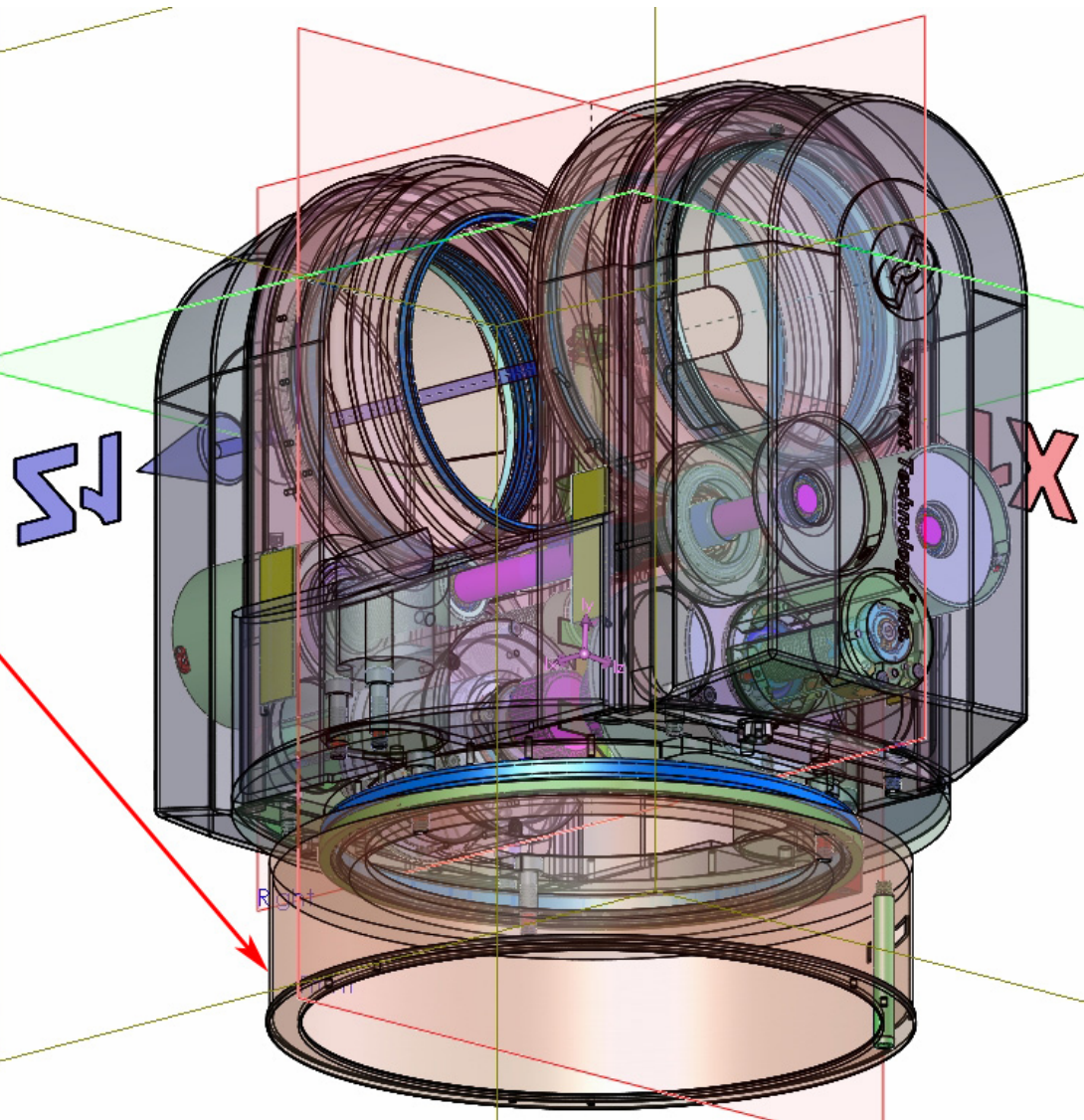
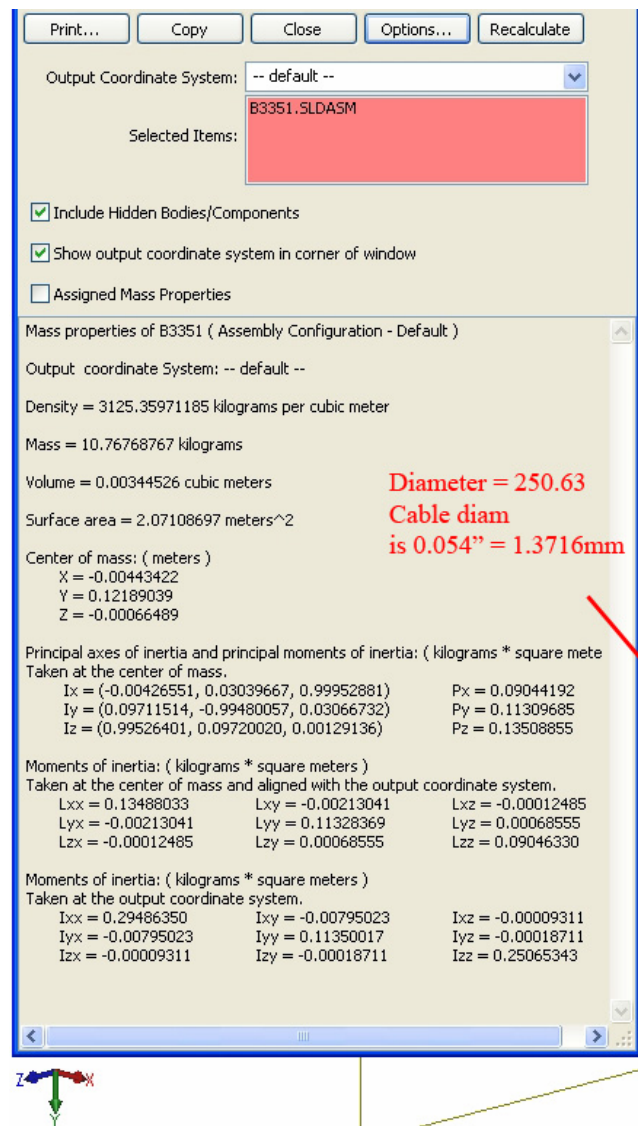


Figure 5 -- Frame-1 Inertia.

Table 3 --Frame-1 Mass properties of B3351 (Assembly Configuration - Default)

Density = 3125.35971185 kilograms per cubic meter

Mass = 10.76768767 kilograms

Volume = 0.00344526 cubic meters

Surface area = 2.07108697 meters²

Center of mass: (meters)

X = -0.00443422

Y = 0.12189039

Z = -0.00066489

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (-0.00426551, 0.03039667, 0.99952881) P_x = 0.09044192

I_y = (0.09711514, -0.99480057, 0.03066732) P_y = 0.11309685

I_z = (0.99526401, 0.09720020, 0.00129136) P_z = 0.13508855

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.13488033 L_{xy} = -0.00213041 L_{xz} = -0.00012485

L_{yx} = -0.00213041 L_{yy} = 0.11328369 L_{yz} = 0.00068555

L_{zx} = -0.00012485 L_{zy} = 0.00068555 L_{zz} = 0.09046330

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.29486350 I_{xy} = -0.00795023 I_{xz} = -0.00009311

I_{yx} = -0.00795023 I_{yy} = 0.11350017 I_{yz} = -0.00018711

I_{zx} = -0.00009311 I_{zy} = -0.00018711 I_{zz} = 0.25065343

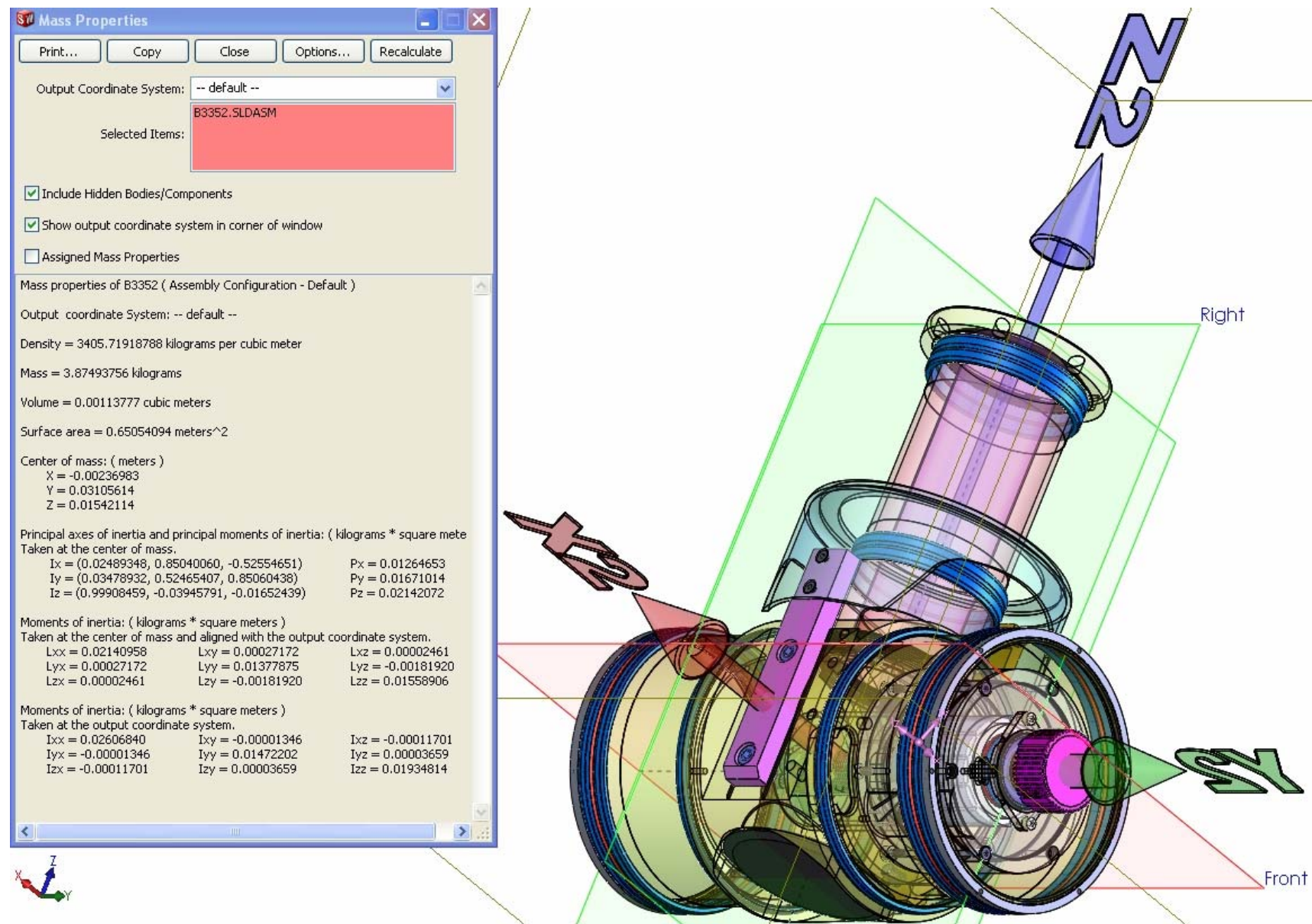


Figure 6 -- Frame-2 Inertia.

Table 4 --Frame-2 Mass properties of B3352 (Assembly Configuration - Default)

Mass = 3.87493756 kilograms

Volume = 0.00113777 cubic meters

Surface area = 0.65054094 meters²

Center of mass: (meters)

X = -0.00236983

Y = 0.03105614

Z = 0.01542114

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.02489348, 0.85040060, -0.52554651)$ $P_x = 0.01264653$

$I_y = (0.03478932, 0.52465407, 0.85060438)$ $P_y = 0.01671014$

$I_z = (0.99908459, -0.03945791, -0.01652439)$ $P_z = 0.02142072$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.02140958$ $L_{xy} = 0.00027172$ $L_{xz} = 0.00002461$

$L_{yx} = 0.00027172$ $L_{yy} = 0.01377875$ $L_{yz} = -0.00181920$

$L_{zx} = 0.00002461$ $L_{zy} = -0.00181920$ $L_{zz} = 0.01558906$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.02606840$ $I_{xy} = -0.00001346$ $I_{xz} = -0.00011701$

$I_{yx} = -0.00001346$ $I_{yy} = 0.01472202$ $I_{yz} = 0.00003659$

$I_{zx} = -0.00011701$ $I_{zy} = 0.00003659$ $I_{zz} = 0.01934814$

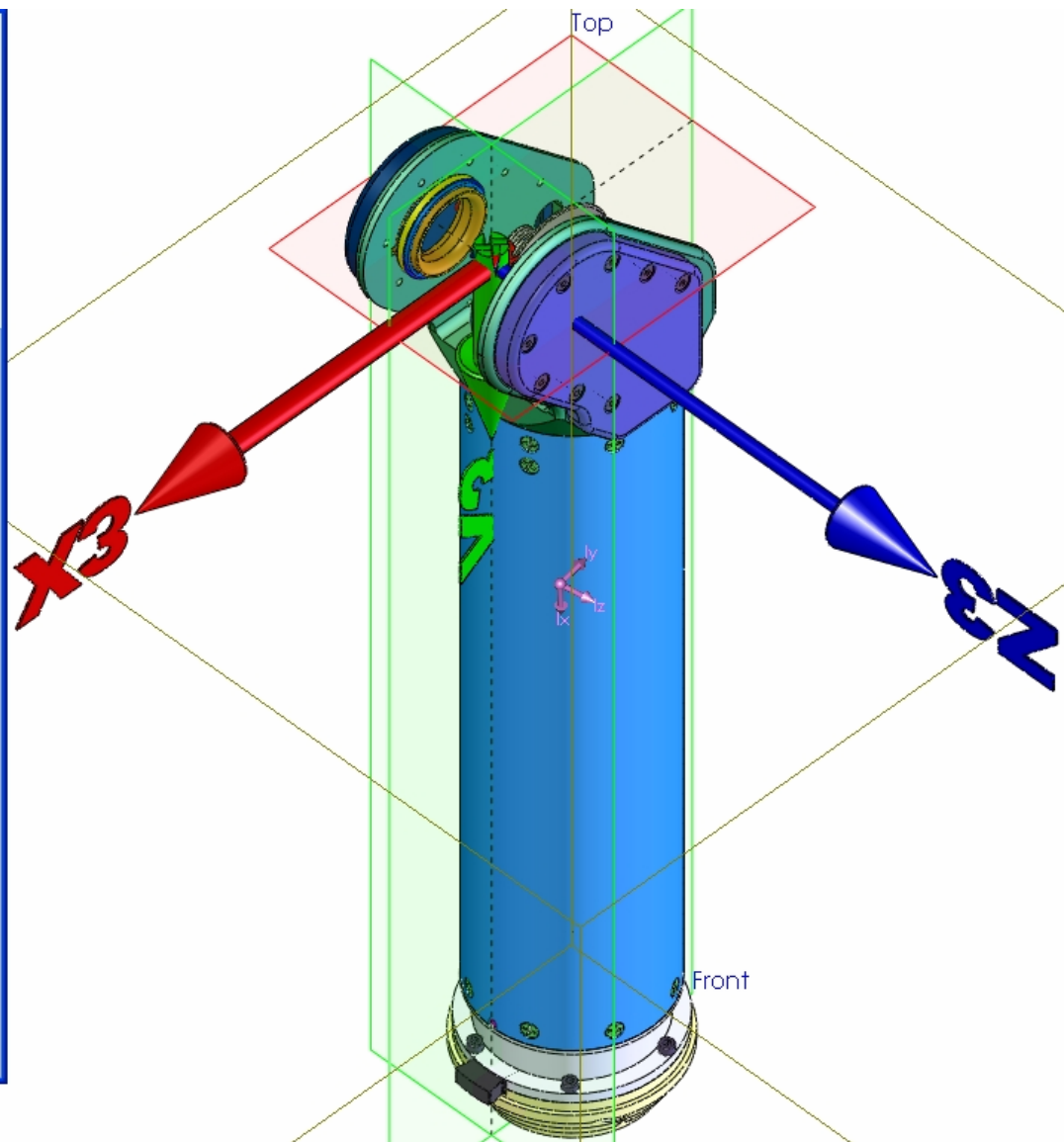
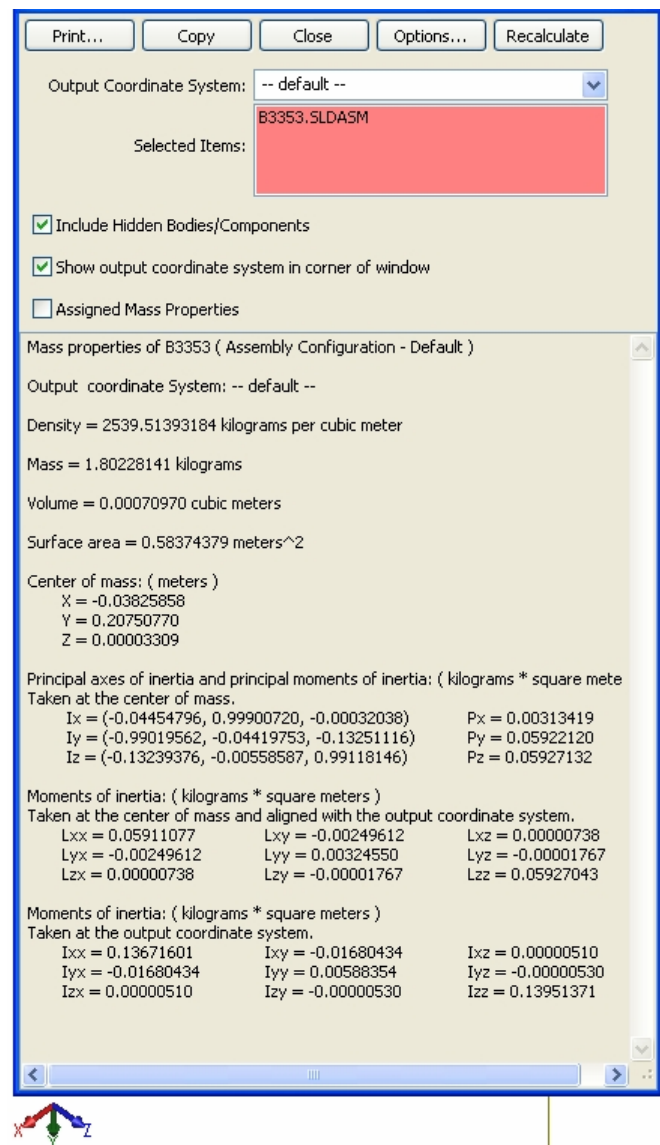


Figure 7 -- Frame-3 Inertia.

Table 5 --Frame-3 Mass properties of B3353 (Assembly Configuration - Default)

Density = 2539.51393184 kilograms per cubic meter

Mass = 1.80228141 kilograms

Volume = 0.00070970 cubic meters

Surface area = 0.58374379 meters²

Center of mass: (meters)

X = -0.03825858

Y = 0.20750770

Z = 0.00003309

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (-0.04454796, 0.99900720, -0.00032038)$ $P_x = 0.00313419$

$I_y = (-0.99019562, -0.04419753, -0.13251116)$ $P_y = 0.05922120$

$I_z = (-0.13239376, -0.00558587, 0.99118146)$ $P_z = 0.05927132$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.05911077$ $L_{xy} = -0.00249612$ $L_{xz} = 0.00000738$

$L_{yx} = -0.00249612$ $L_{yy} = 0.00324550$ $L_{yz} = -0.00001767$

$L_{zx} = 0.00000738$ $L_{zy} = -0.00001767$ $L_{zz} = 0.05927043$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.13671601$ $I_{xy} = -0.01680434$ $I_{xz} = 0.00000510$

$I_{yx} = -0.01680434$ $I_{yy} = 0.00588354$ $I_{yz} = -0.00000530$

$I_{zx} = 0.00000510$ $I_{zy} = -0.00000530$ $I_{zz} = 0.13951371$

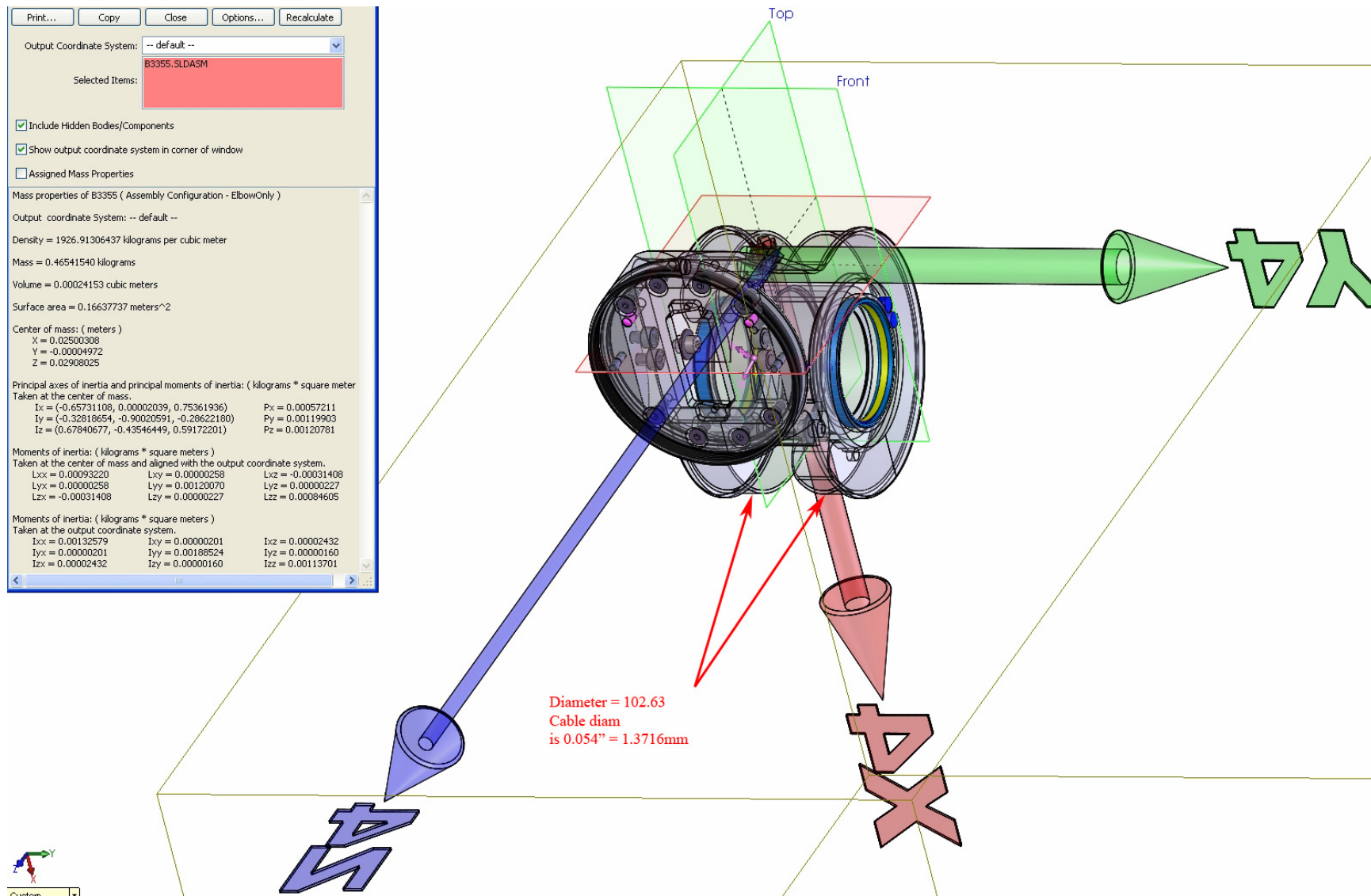


Figure 8 -- Frame-4 Inertia (without any attachment)

Table 6 --Frame-4 Mass properties of B3355 (Assembly Configuration - ElbowOnly)

Density = 1926.91306437 kilograms per cubic meter

Mass = 0.46541540 kilograms

Volume = 0.00024153 cubic meters

Surface area = 0.16637737 meters²

Center of mass: (meters)

X = 0.02500308

Y = -0.00004972

Z = 0.02908025

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (-0.65731108, 0.00002039, 0.75361936) P_x = 0.00057211

I_y = (-0.32818654, -0.90020591, -0.28622180) P_y = 0.00119903

I_z = (0.67840677, -0.43546449, 0.59172201) P_z = 0.00120781

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.00093220 L_{xy} = 0.00000258 L_{xz} = -0.00031408

L_{yx} = 0.00000258 L_{yy} = 0.00120070 L_{yz} = 0.00000227

L_{zx} = -0.00031408 L_{zy} = 0.00000227 L_{zz} = 0.00084605

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.00132579 I_{xy} = 0.00000201 I_{xz} = 0.00002432

I_{yx} = 0.00000201 I_{yy} = 0.00188524 I_{yz} = 0.00000160

I_{zx} = 0.00002432 I_{zy} = 0.00000160 I_{zz} = 0.00113701

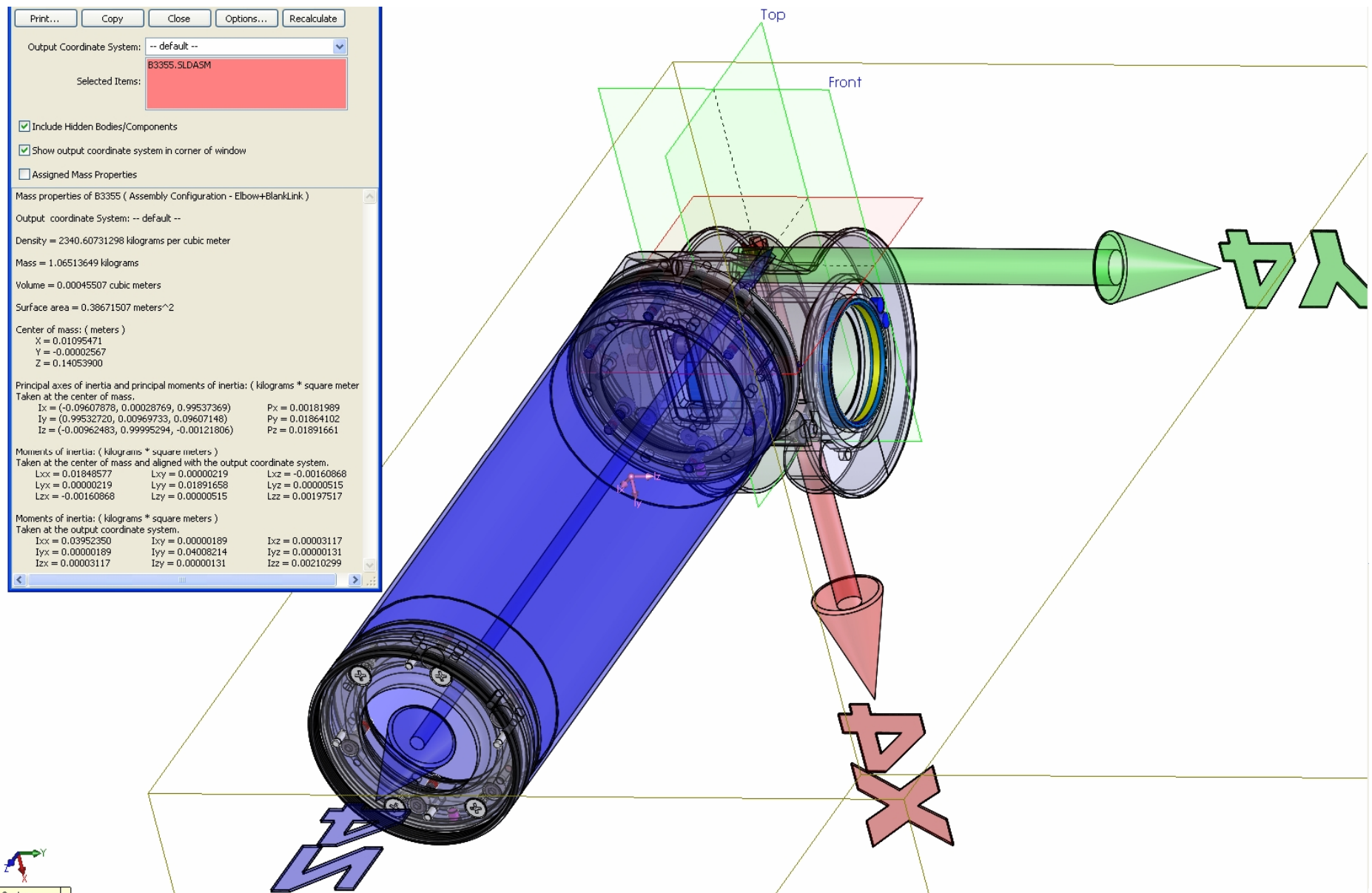


Table 7 --Frame-4 Mass properties of B3355 (Assembly Configuration - Elbow+BlankLink)

Density = 2340.60731298 kilograms per cubic meter

Mass = 1.06513649 kilograms

Volume = 0.00045507 cubic meters

Surface area = 0.38671507 meters²

Center of mass: (meters)

X = 0.01095471

Y = -0.00002567

Z = 0.14053900

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (-0.09607878, 0.00028769, 0.99537369) P_x = 0.00181989

I_y = (0.99532720, 0.00969733, 0.09607148) P_y = 0.01864102

I_z = (-0.00962483, 0.99995294, -0.00121806) P_z = 0.01891661

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.01848577 L_{xy} = 0.00000219 L_{xz} = -0.00160868

L_{yx} = 0.00000219 L_{yy} = 0.01891658 L_{yz} = 0.00000515

L_{zx} = -0.00160868 L_{zy} = 0.00000515 L_{zz} = 0.00197517

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.03952350 I_{xy} = 0.00000189 I_{xz} = 0.00003117

I_{yx} = 0.00000189 I_{yy} = 0.04008214 I_{yz} = 0.00000131

I_{zx} = 0.00003117 I_{zy} = 0.00000131 I_{zz} = 0.00210299

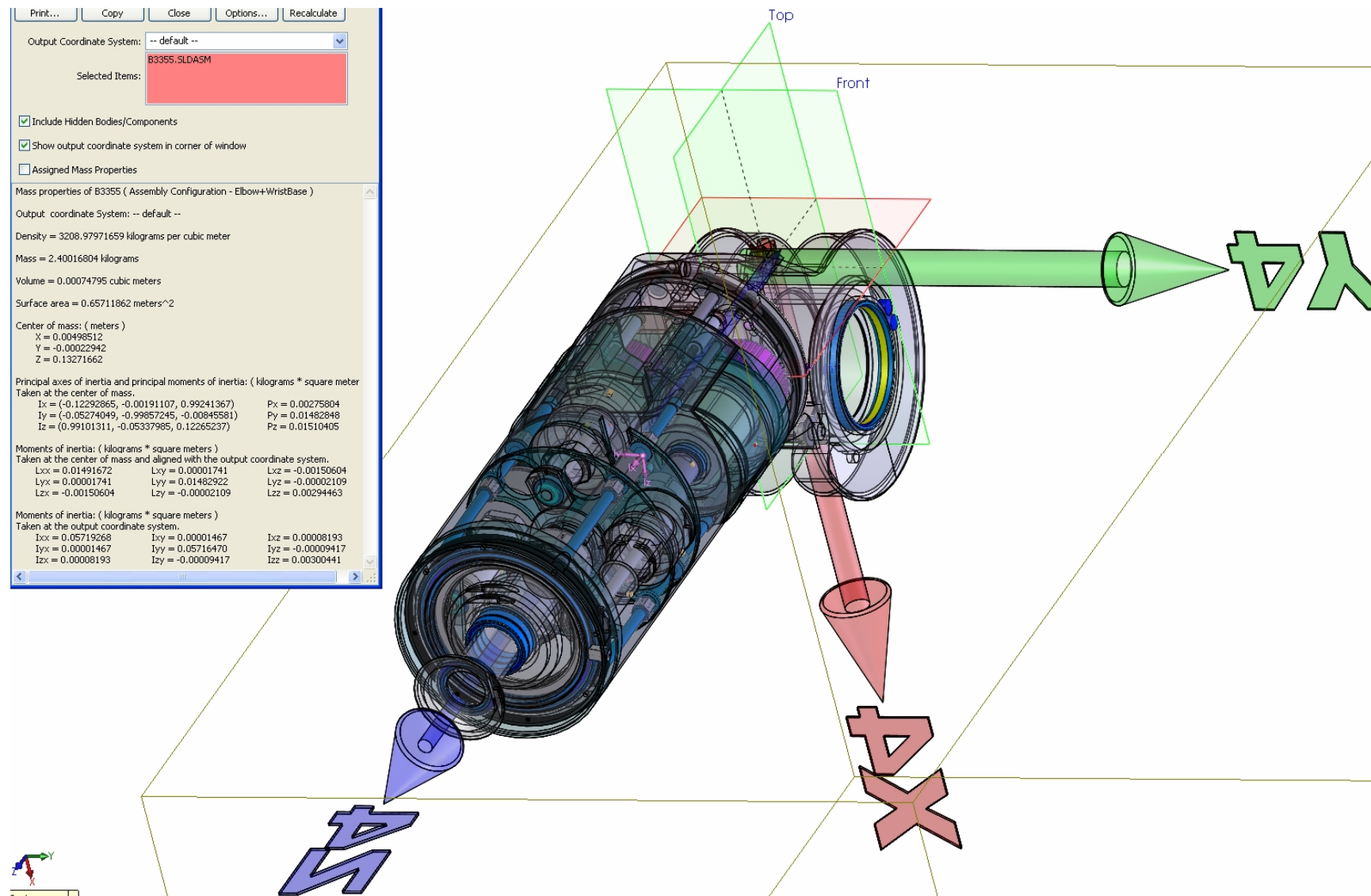


Figure 10 -- Frame-4 Inertia (with base of wrist attached).

Table 8 --Frame-4 Mass properties of B3355 (Assembly Configuration - Elbow+WristBase)

Density = 3208.97971659 kilograms per cubic meter

Mass = 2.40016804 kilograms

Volume = 0.00074795 cubic meters

Surface area = 0.65711862 meters²

Center of mass: (meters)

X = 0.00498512

Y = -0.00022942

Z = 0.13271662

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (-0.12292865, -0.00191107, 0.99241367) P_x = 0.00275804

I_y = (-0.05274049, -0.99857245, -0.00845581) P_y = 0.01482848

I_z = (0.99101311, -0.05337985, 0.12265237) P_z = 0.01510405

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.01491672 L_{xy} = 0.00001741 L_{xz} = -0.00150604

L_{yx} = 0.00001741 L_{yy} = 0.01482922 L_{yz} = -0.00002109

L_{zx} = -0.00150604 L_{zy} = -0.00002109 L_{zz} = 0.00294463

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.05719268 I_{xy} = 0.00001467 I_{xz} = 0.00008193

I_{yx} = 0.00001467 I_{yy} = 0.05716470 I_{yz} = -0.00009417

I_{zx} = 0.00008193 I_{zy} = -0.00009417 I_{zz} = 0.00300441

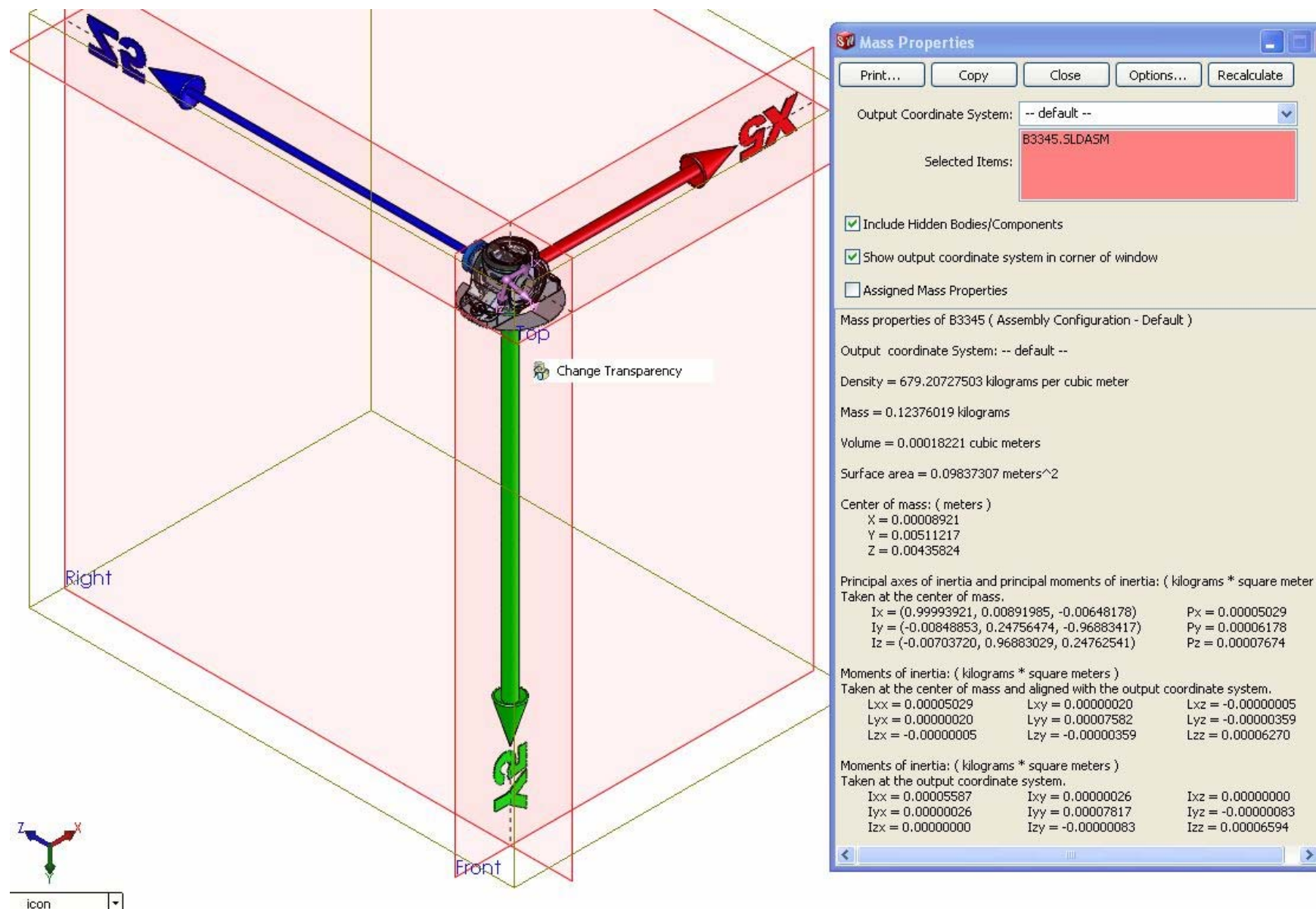


Figure 11 – Frame-5 Inertia

Table 9 --Frame-5 Mass properties of B3345 (Assembly Configuration - Default)

Density = 679.20727503 kilograms per cubic meter

Mass = 0.12376019 kilograms

Volume = 0.00018221 cubic meters

Surface area = 0.09837307 meters²

Center of mass: (meters)

X = 0.00008921

Y = 0.00511217

Z = 0.00435824

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.99993921, 0.00891985, -0.00648178)$ $P_x = 0.00005029$

$I_y = (-0.00848853, 0.24756474, -0.96883417)$ $P_y = 0.00006178$

$I_z = (-0.00703720, 0.96883029, 0.24762541)$ $P_z = 0.00007674$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00005029$ $L_{xy} = 0.00000020$ $L_{xz} = -0.00000005$

$L_{yx} = 0.00000020$ $L_{yy} = 0.00007582$ $L_{yz} = -0.00000359$

$L_{zx} = -0.00000005$ $L_{zy} = -0.00000359$ $L_{zz} = 0.00006270$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00005587$ $I_{xy} = 0.00000026$ $I_{xz} = 0.00000000$

$I_{yx} = 0.00000026$ $I_{yy} = 0.00007817$ $I_{yz} = -0.00000083$

$I_{zx} = 0.00000000$ $I_{zy} = -0.00000083$ $I_{zz} = 0.00006594$

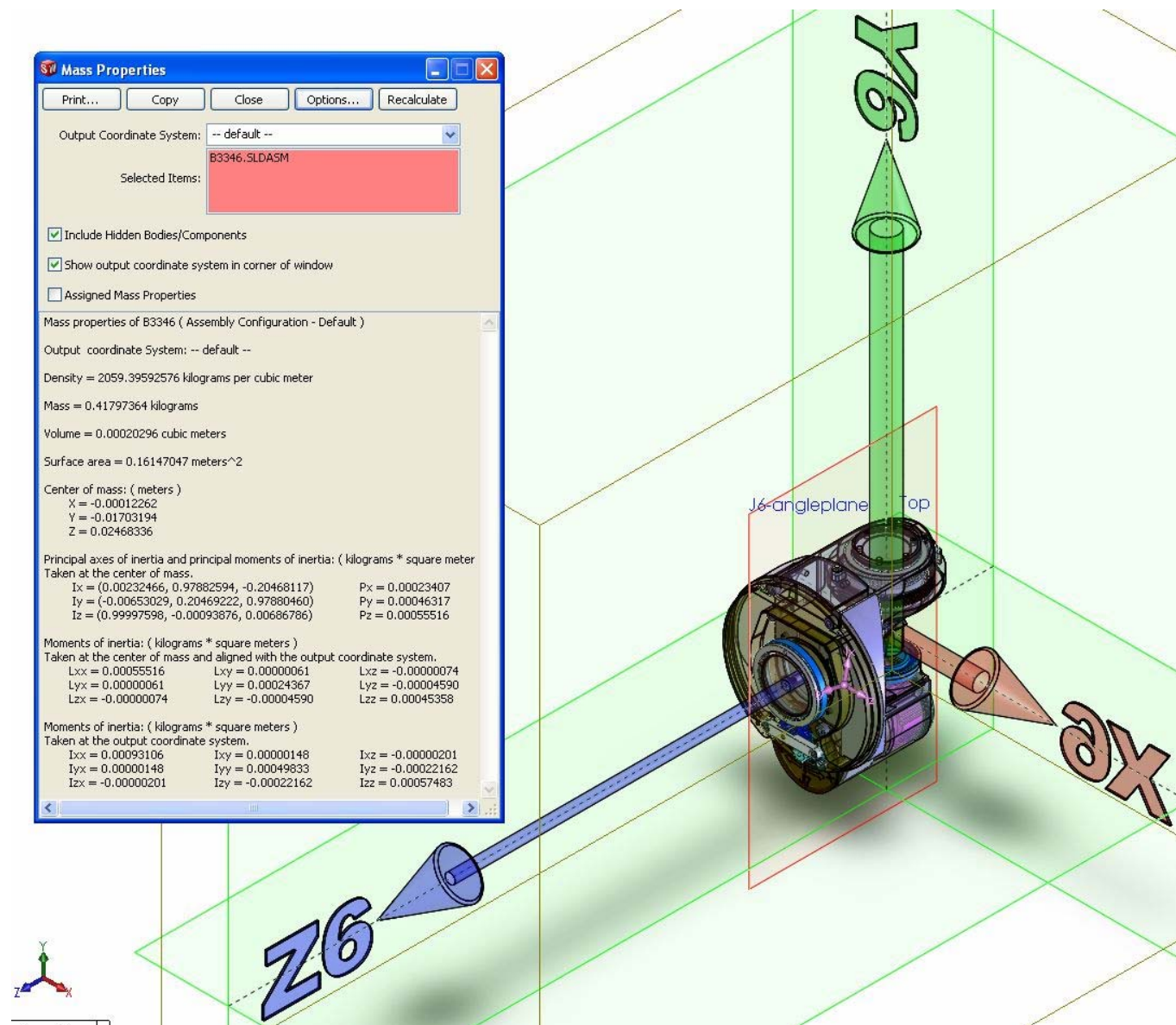


Figure 12 -- Frame-6 Inertia.

Table 10 --Frame-6 Mass properties of B3346 (Assembly Configuration - Default)

Density = 2059.39592576 kilograms per cubic meter

Mass = 0.41797364 kilograms

Volume = 0.00020296 cubic meters

Surface area = 0.16147047 meters²

Center of mass: (meters)

X = -0.00012262

Y = -0.01703194

Z = 0.02468336

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.00232466, 0.97882594, -0.20468117)$ $P_x = 0.00023407$

$I_y = (-0.00653029, 0.20469222, 0.97880460)$ $P_y = 0.00046317$

$I_z = (0.99997598, -0.00093876, 0.00686786)$ $P_z = 0.00055516$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00055516$ $L_{xy} = 0.00000061$ $L_{xz} = -0.00000074$

$L_{yx} = 0.00000061$ $L_{yy} = 0.00024367$ $L_{yz} = -0.00004590$

$L_{zx} = -0.00000074$ $L_{zy} = -0.00004590$ $L_{zz} = 0.00045358$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00093106$ $I_{xy} = 0.00000148$ $I_{xz} = -0.00000201$

$I_{yx} = 0.00000148$ $I_{yy} = 0.00049833$ $I_{yz} = -0.00022162$

$I_{zx} = -0.00000201$ $I_{zy} = -0.00022162$ $I_{zz} = 0.00057483$

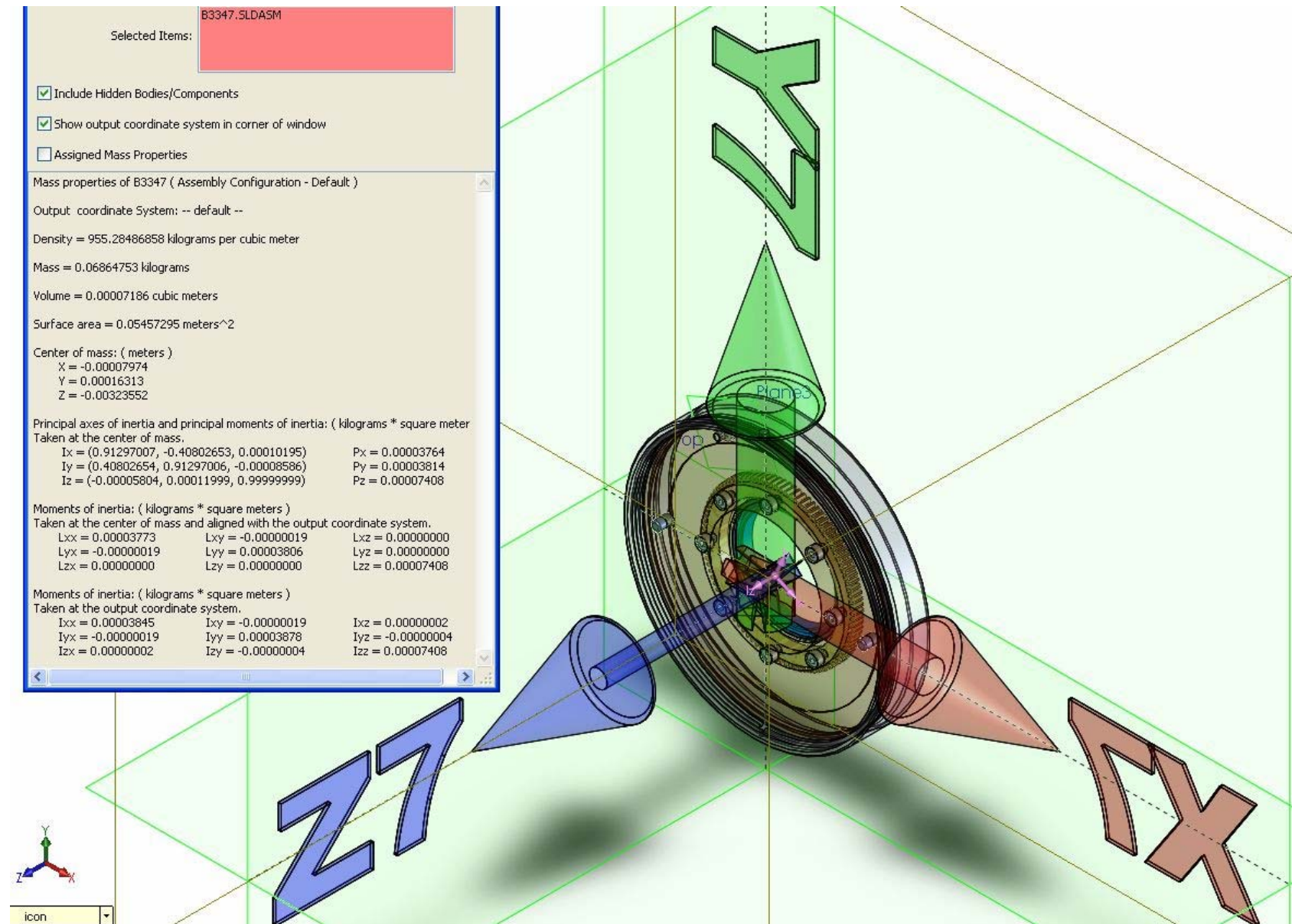


Figure 13 -- Frame-7 Inertia.

Table 11 --Frame-7 Mass properties of B3347 (Assembly Configuration - Default)

Density = 955.28486858 kilograms per cubic meter

Mass = 0.06864753 kilograms

Volume = 0.00007186 cubic meters

Surface area = 0.05457295 meters²

Center of mass: (meters)

X = -0.00007974

Y = 0.00016313

Z = -0.00323552

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.91297007, -0.40802653, 0.00010195)$ $P_x = 0.00003764$

$I_y = (0.40802654, 0.91297006, -0.00008586)$ $P_y = 0.00003814$

$I_z = (-0.00005804, 0.00011999, 0.99999999)$ $P_z = 0.00007408$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00003773$ $L_{xy} = -0.00000019$ $L_{xz} = 0.00000000$

$L_{yx} = -0.00000019$ $L_{yy} = 0.00003806$ $L_{yz} = 0.00000000$

$L_{zx} = 0.00000000$ $L_{zy} = 0.00000000$ $L_{zz} = 0.00007408$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00003845$ $I_{xy} = -0.00000019$ $I_{xz} = 0.00000002$

$I_{yx} = -0.00000019$ $I_{yy} = 0.00003878$ $I_{yz} = -0.00000004$

$I_{zx} = 0.00000002$ $I_{zy} = -0.00000004$ $I_{zz} = 0.00007408$

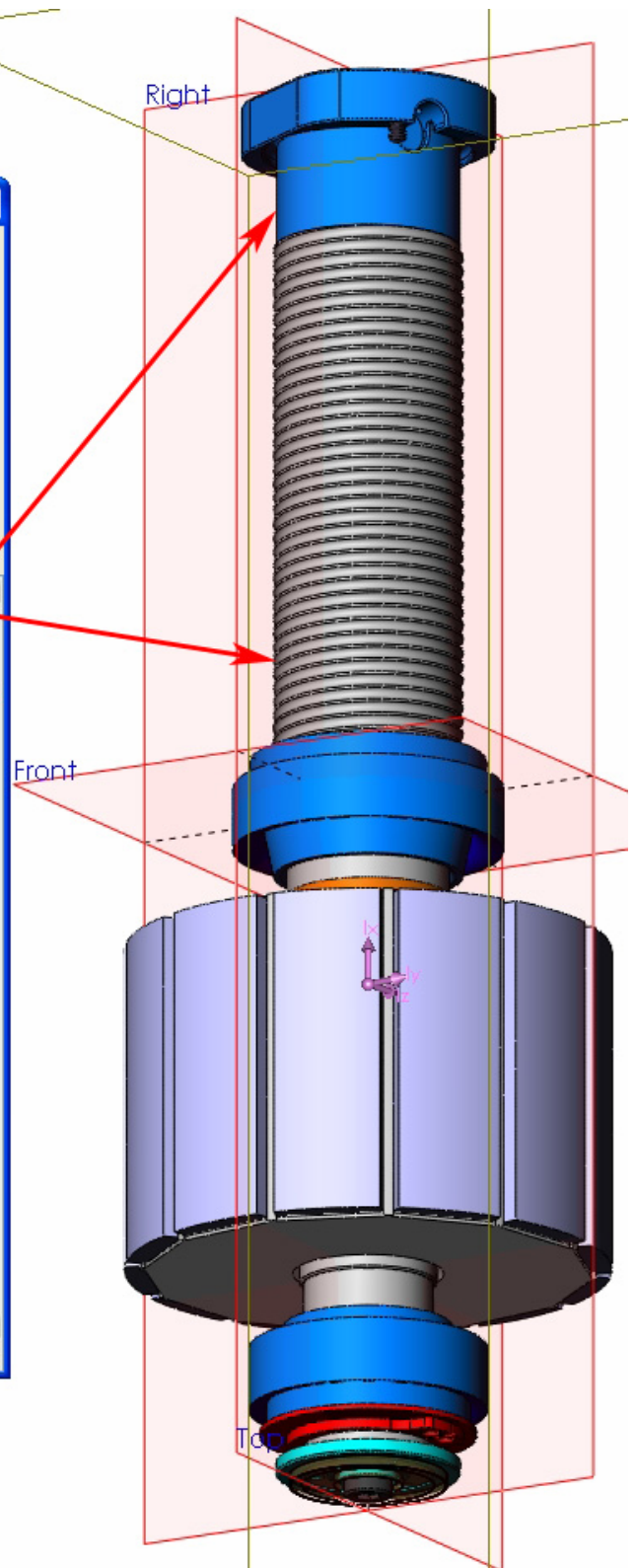
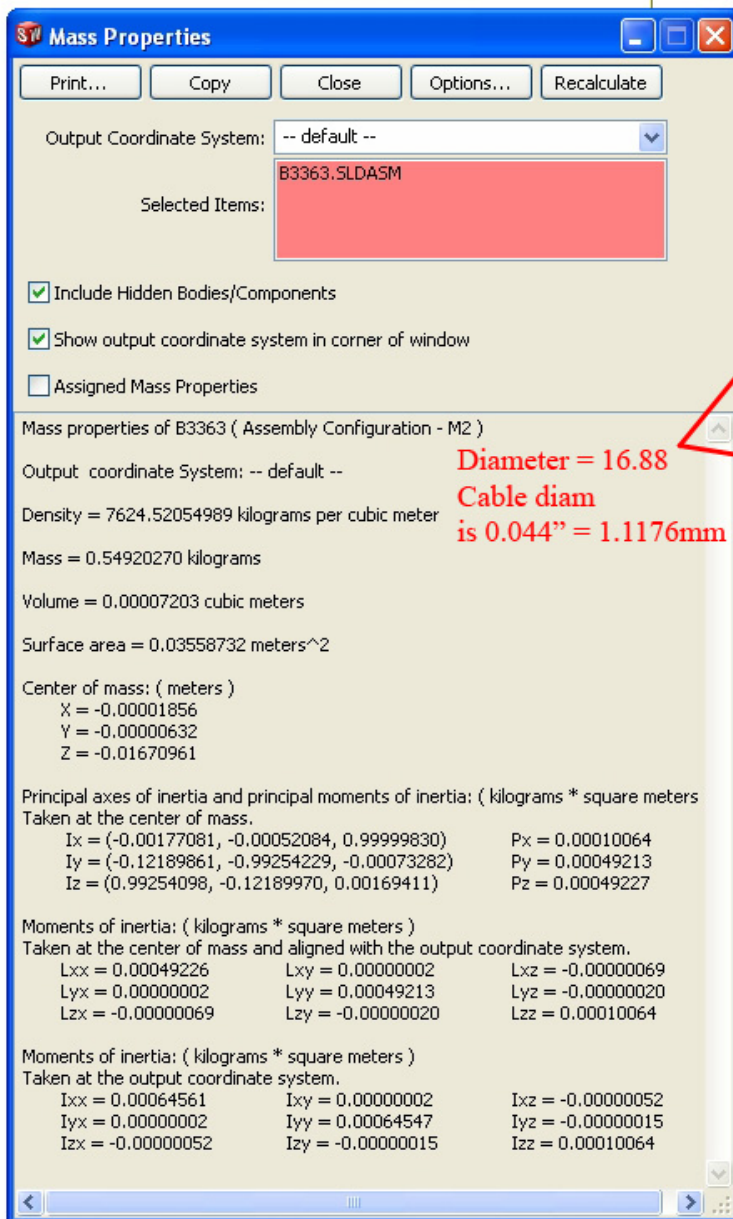


Figure 14 -- Motor Rotor for the 1st Four DOFs of the WAM.

Table 12 --Mass properties of B3363 (Assembly Configuration - M2)

Density = 7624.52054989 kilograms per cubic meter

Mass = 0.54920270 kilograms

Volume = 0.00007203 cubic meters

Surface area = 0.03558732 meters²

Center of mass: (meters)

X = -0.00001856

Y = -0.00000632

Z = -0.01670961

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (-0.00177081, -0.00052084, 0.99999830) P_x = 0.00010064

I_y = (-0.12189861, -0.99254229, -0.00073282) P_y = 0.00049213

I_z = (0.99254098, -0.12189970, 0.00169411) P_z = 0.00049227

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.00049226 L_{xy} = 0.00000002 L_{xz} = -0.00000069

L_{yx} = 0.00000002 L_{yy} = 0.00049213 L_{yz} = -0.00000020

L_{zx} = -0.00000069 L_{zy} = -0.00000020 L_{zz} = 0.00010064

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.00064561 I_{xy} = 0.00000002 I_{xz} = -0.00000052

I_{yx} = 0.00000002 I_{yy} = 0.00064547 I_{yz} = -0.00000015

I_{zx} = -0.00000052 I_{zy} = -0.00000015 **I_{zz} = 0.00010064**

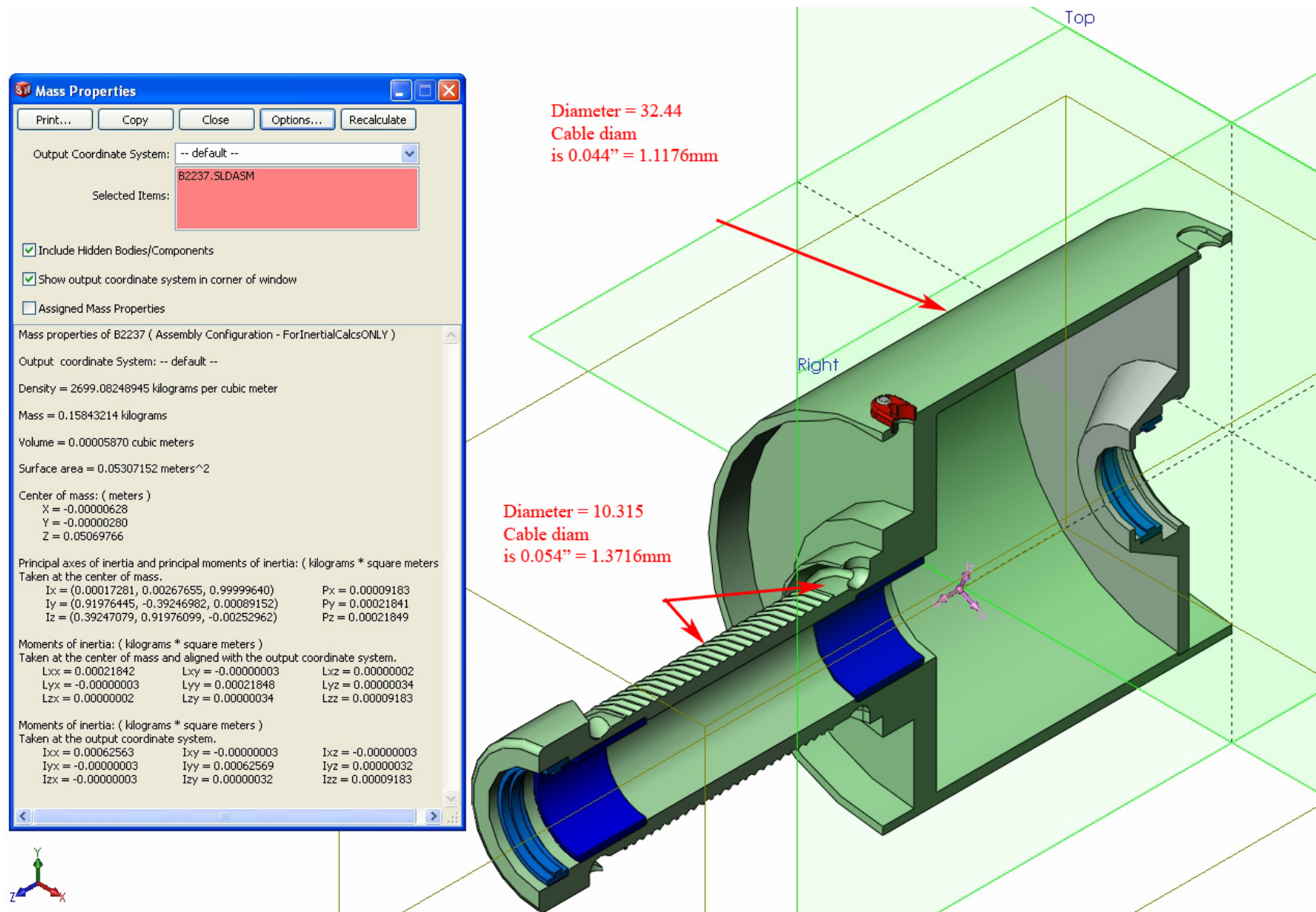


Figure 15 -- "Grenade" that couples 1st and 2nd stages of the 1st three DOFs of the WAM.

Table 13 --Mass properties of B2237 (Assembly Configuration - ForInertialCalcsONLY)

Density = 2699.08248945 kilograms per cubic meter

Mass = 0.15843214 kilograms

Volume = 0.00005870 cubic meters

Surface area = 0.05307152 meters²

Center of mass: (meters)

X = -0.00000628

Y = -0.00000280

Z = 0.05069766

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.00017281, 0.00267655, 0.99999640)$ $P_x = 0.00009183$

$I_y = (0.91976445, -0.39246982, 0.00089152)$ $P_y = 0.00021841$

$I_z = (0.39247079, 0.91976099, -0.00252962)$ $P_z = 0.00021849$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00021842$ $L_{xy} = -0.00000003$ $L_{xz} = 0.00000002$

$L_{yx} = -0.00000003$ $L_{yy} = 0.00021848$ $L_{yz} = 0.00000034$

$L_{zx} = 0.00000002$ $L_{zy} = 0.00000034$ $L_{zz} = 0.00009183$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00062563$ $I_{xy} = -0.00000003$ $I_{xz} = -0.00000003$

$I_{yx} = -0.00000003$ $I_{yy} = 0.00062569$ $I_{yz} = 0.00000032$

$I_{zx} = -0.00000003$ $I_{zy} = 0.00000032$ **$I_{zz} = 0.00009183$**

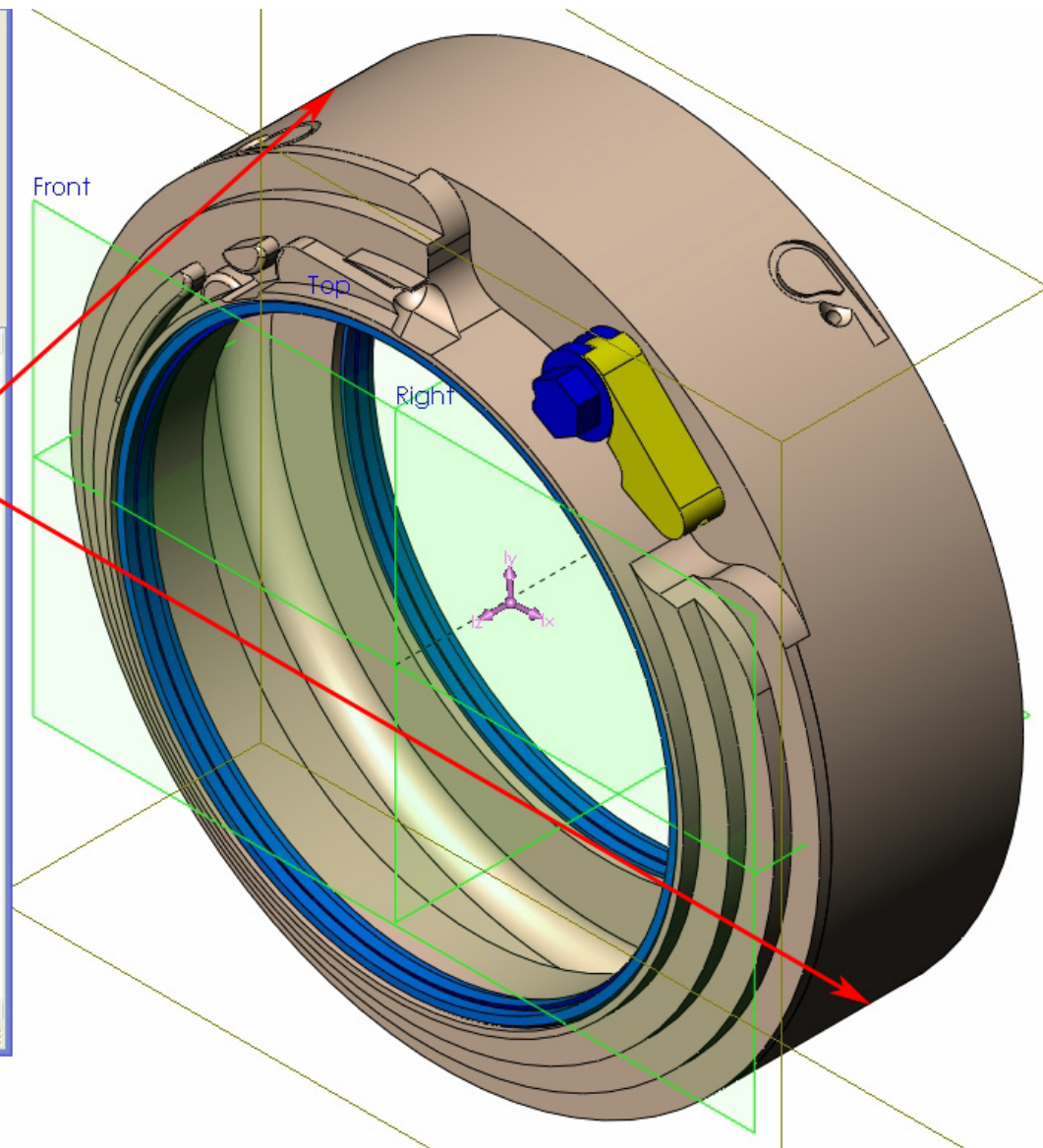
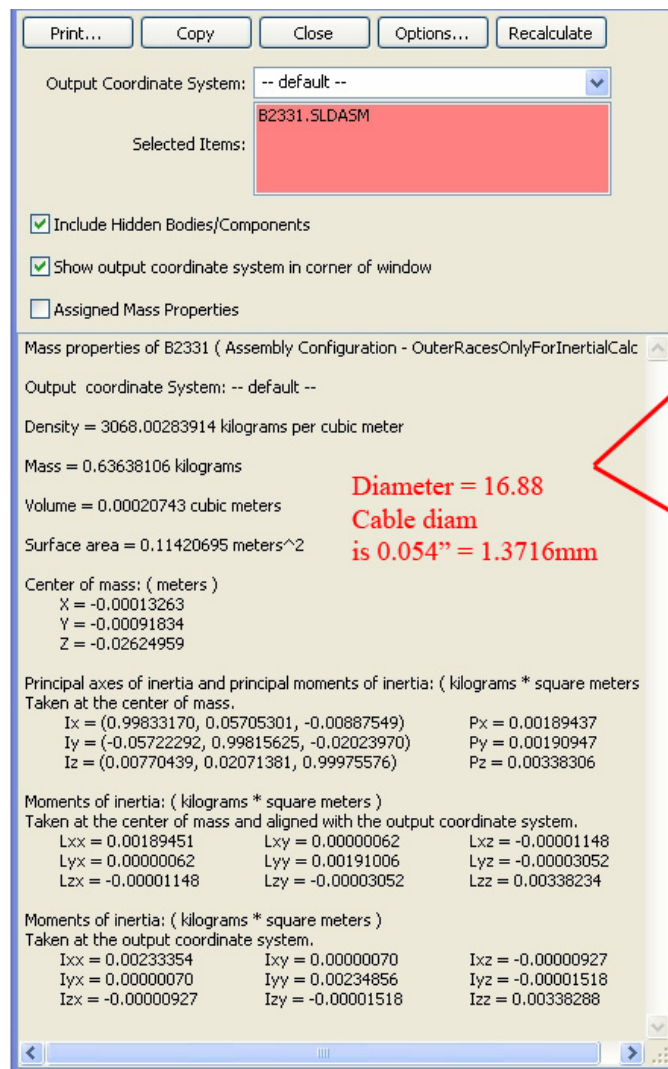


Figure 16 -- Differential-Input Pulley.

Table 14 --Mass properties of B2331 (Assembly Configuration - OuterRacesOnlyForInertialCalcs)

Density = 3068.00283914 kilograms per cubic meter

Mass = 0.63638106 kilograms

Volume = 0.00020743 cubic meters

Surface area = 0.11420695 meters²

Center of mass: (meters)

X = -0.00013263

Y = -0.00091834

Z = -0.02624959

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (0.99833170, 0.05705301, -0.00887549) P_x = 0.00189437

I_y = (-0.05722292, 0.99815625, -0.02023970) P_y = 0.00190947

I_z = (0.00770439, 0.02071381, 0.99975576) P_z = 0.00338306

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.00189451 L_{xy} = 0.00000062 L_{xz} = -0.00001148

L_{yx} = 0.00000062 L_{yy} = 0.00191006 L_{yz} = -0.00003052

L_{zx} = -0.00001148 L_{zy} = -0.00003052 L_{zz} = 0.00338234

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.00233354 I_{xy} = 0.00000070 I_{xz} = -0.00000927

I_{yx} = 0.00000070 I_{yy} = 0.00234856 I_{yz} = -0.00001518

I_{zx} = -0.00000927 I_{zy} = -0.00001518 **I_{zz} = 0.00338288**

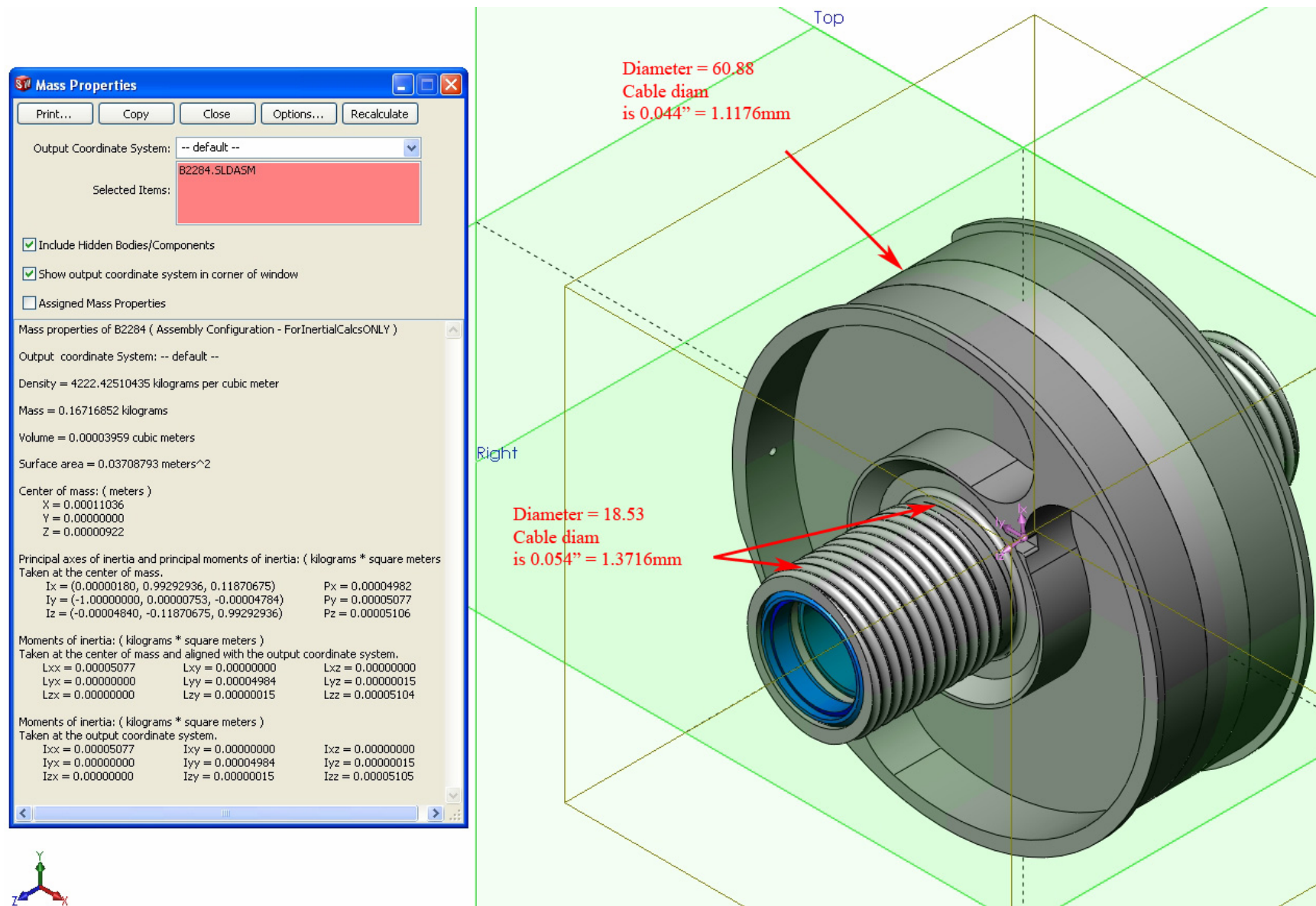


Figure 17 -- Elbow Pulley-Pinion with all bearings that couples the 1st & 2nd stages of J4.

Table 15 --Mass properties of B2284 (Assembly Configuration - ForInertialCalcsONLY)

Density = 4222.42510435 kilograms per cubic meter

Mass = 0.16716852 kilograms

Volume = 0.00003959 cubic meters

Surface area = 0.03708793 meters²

Center of mass: (meters)

X = 0.00011036

Y = 0.00000000

Z = 0.00000922

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.00000180, 0.99292936, 0.11870675)$ $P_x = 0.00004982$

$I_y = (-1.00000000, 0.00000753, -0.00004784)$ $P_y = 0.00005077$

$I_z = (-0.00004840, -0.11870675, 0.99292936)$ $P_z = 0.00005106$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00005077$ $L_{xy} = 0.00000000$ $L_{xz} = 0.00000000$

$L_{yx} = 0.00000000$ $L_{yy} = 0.00004984$ $L_{yz} = 0.00000015$

$L_{zx} = 0.00000000$ $L_{zy} = 0.00000015$ $L_{zz} = 0.00005104$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00005077$ $I_{xy} = 0.00000000$ $I_{xz} = 0.00000000$

$I_{yx} = 0.00000000$ $I_{yy} = 0.00004984$ $I_{yz} = 0.00000015$

$I_{zx} = 0.00000000$ $I_{zy} = 0.00000015$ **$I_{zz} = 0.00005105$**

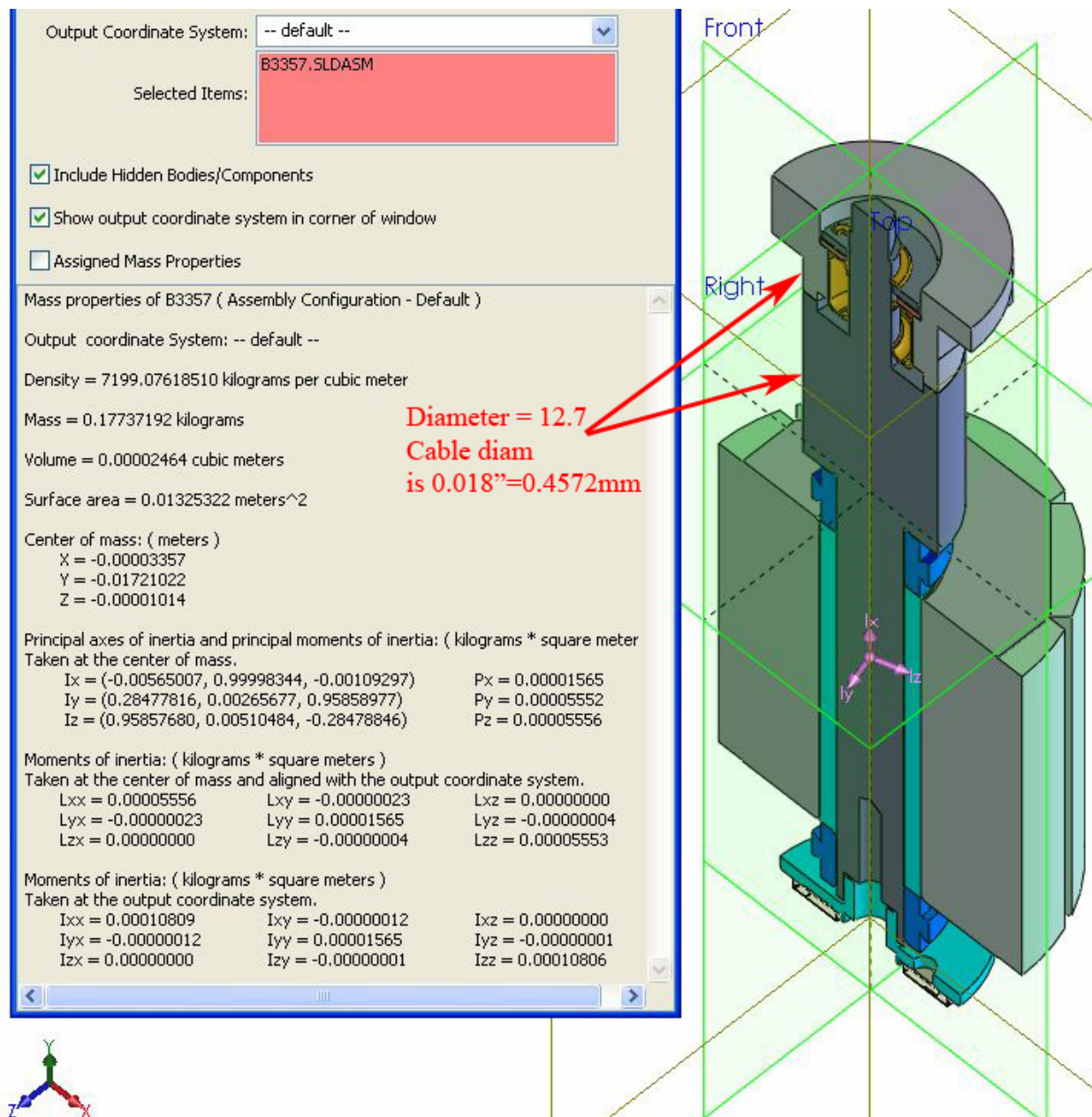


Figure 18 -- M5/M6 Motor Inertia.

Table 16 --Mass properties of B3357 (Assembly Configuration - Default)

Density = 7199.07618510 kilograms per cubic meter

Mass = 0.17737192 kilograms

Volume = 0.00002464 cubic meters

Surface area = 0.01325322 meters²

Center of mass: (meters)

X = -0.00003357

Y = -0.01721022

Z = -0.00001014

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (-0.00565007, 0.99998344, -0.00109297)$ $P_x = 0.00001565$

$I_y = (0.28477816, 0.00265677, 0.95858977)$ $P_y = 0.00005552$

$I_z = (0.95857680, 0.00510484, -0.28478846)$ $P_z = 0.00005556$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00005556$ $L_{xy} = -0.00000023$ $L_{xz} = 0.00000000$

$L_{yx} = -0.00000023$ $L_{yy} = 0.00001565$ $L_{yz} = -0.00000004$

$L_{zx} = 0.00000000$ $L_{zy} = -0.00000004$ $L_{zz} = 0.00005553$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00010809$ $I_{xy} = -0.00000012$ $I_{xz} = 0.00000000$

$I_{yx} = -0.00000012$ **$I_{yy} = 0.00001565$** $I_{yz} = -0.00000001$

$I_{zx} = 0.00000000$ $I_{zy} = -0.00000001$ $I_{zz} = 0.00010806$

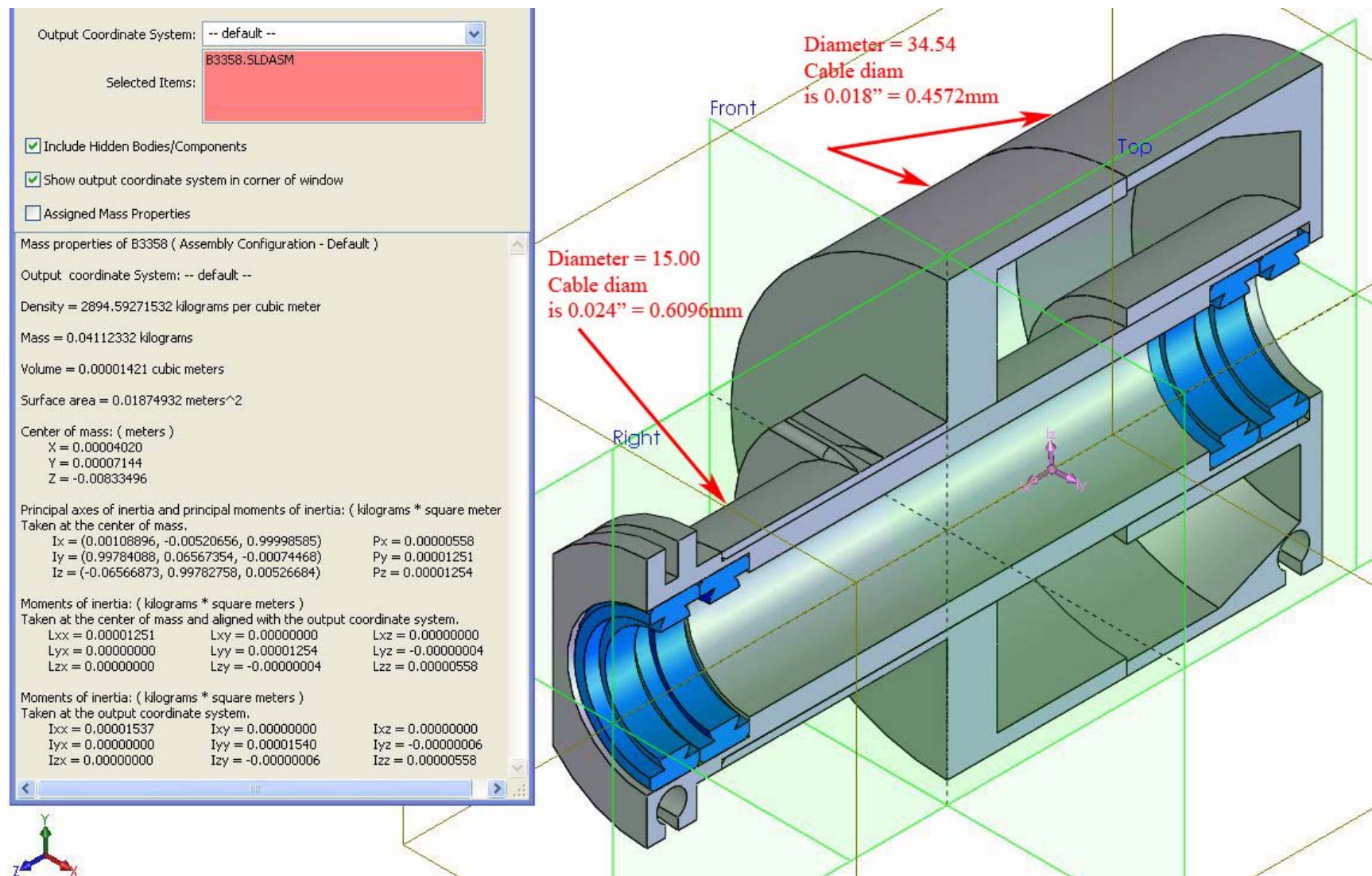


Figure 19 -- Stage-1-2 PulleyPinion.

Table 17 --Mass properties of B3358 (Assembly Configuration - Default)

Density = 2894.59271532 kilograms per cubic meter

Mass = 0.04112332 kilograms

Volume = 0.00001421 cubic meters

Surface area = 0.01874932 meters²

Center of mass: (meters)

X = 0.00004020

Y = 0.00007144

Z = -0.00833496

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.00108896, -0.00520656, 0.99998585)$ $P_x = 0.00000558$

$I_y = (0.99784088, 0.06567354, -0.00074468)$ $P_y = 0.00001251$

$I_z = (-0.06566873, 0.99782758, 0.00526684)$ $P_z = 0.00001254$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00001251$ $L_{xy} = 0.00000000$ $L_{xz} = 0.00000000$

$L_{yx} = 0.00000000$ $L_{yy} = 0.00001254$ $L_{yz} = -0.00000004$

$L_{zx} = 0.00000000$ $L_{zy} = -0.00000004$ $L_{zz} = 0.00000558$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00001537$ $I_{xy} = 0.00000000$ $I_{xz} = 0.00000000$

$I_{yx} = 0.00000000$ $I_{yy} = 0.00001540$ $I_{yz} = -0.00000006$

$I_{zx} = 0.00000000$ $I_{zy} = -0.00000006$ **$I_{zz} = 0.00000558$**

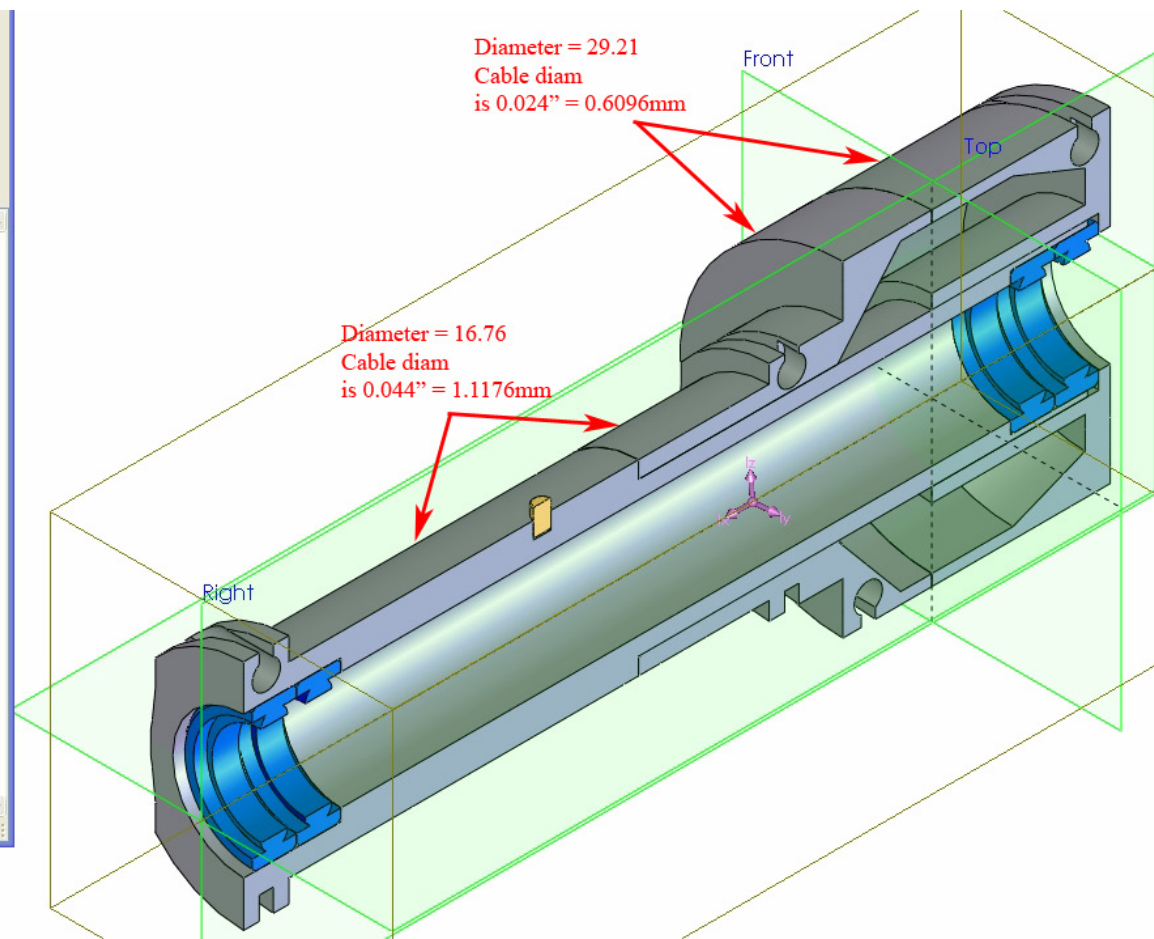
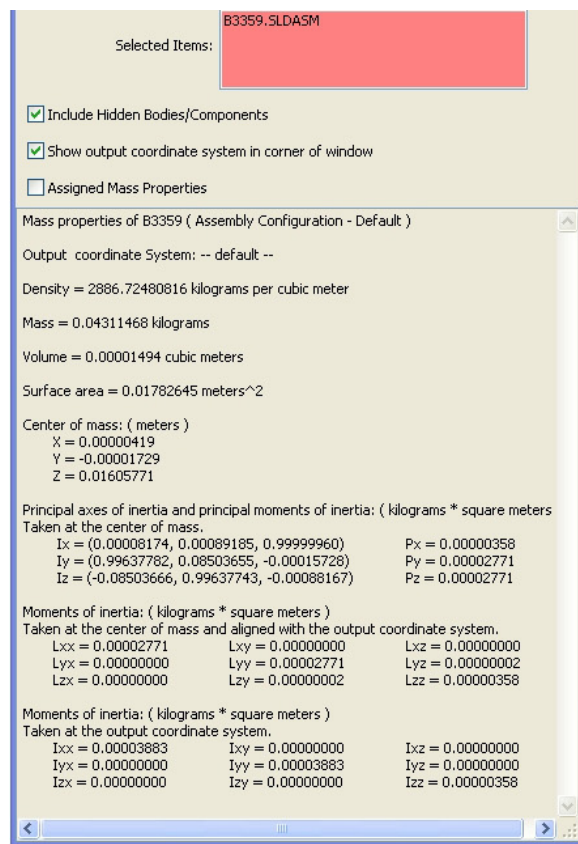


Figure 20 –Stage2-3 PulleyPinion.

Table 18 --Mass properties of B3359 (Assembly Configuration - Default)

Density = 2886.72480816 kilograms per cubic meter

Mass = 0.04311468 kilograms

Volume = 0.00001494 cubic meters

Surface area = 0.01782645 meters²

Center of mass: (meters)

X = 0.00000419

Y = -0.00001729

Z = 0.01605771

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.00008174, 0.00089185, 0.99999960)$ $P_x = 0.00000358$

$I_y = (0.99637782, 0.08503655, -0.00015728)$ $P_y = 0.00002771$

$I_z = (-0.08503666, 0.99637743, -0.00088167)$ $P_z = 0.00002771$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00002771$ $L_{xy} = 0.00000000$ $L_{xz} = 0.00000000$

$L_{yx} = 0.00000000$ $L_{yy} = 0.00002771$ $L_{yz} = 0.00000002$

$L_{zx} = 0.00000000$ $L_{zy} = 0.00000002$ $L_{zz} = 0.00000358$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00003883$ $I_{xy} = 0.00000000$ $I_{xz} = 0.00000000$

$I_{yx} = 0.00000000$ $I_{yy} = 0.00003883$ $I_{yz} = 0.00000000$

$I_{zx} = 0.00000000$ $I_{zy} = 0.00000000$ **$I_{zz} = 0.00000358$**

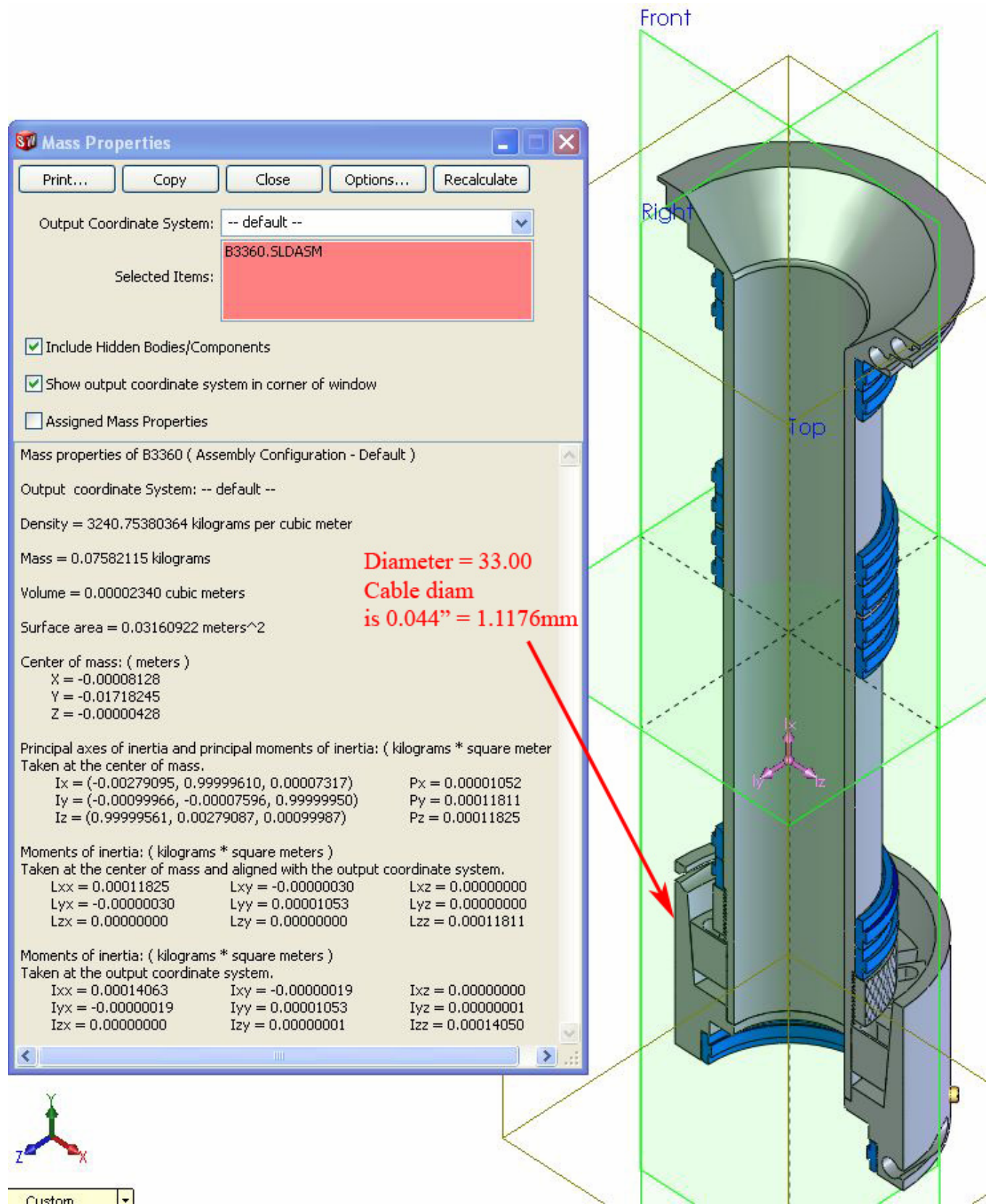


Figure 21 -- Wrist differential outer input-pulley pair driven by Motor 5.

Table 19 -- Mass properties of B3360 (Assembly Configuration - Default)

Density = 3240.75380364 kilograms per cubic meter

Mass = 0.07582115 kilograms

Volume = 0.00002340 cubic meters

Surface area = 0.03160922 meters²

Center of mass: (meters)

X = -0.00008128

Y = -0.01718245

Z = -0.00000428

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (-0.00279095, 0.99999610, 0.00007317) P_x = 0.00001052

I_y = (-0.00099966, -0.00007596, 0.99999950) P_y = 0.00011811

I_z = (0.99999561, 0.00279087, 0.00099987) P_z = 0.00011825

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.00011825 L_{xy} = -0.00000030 L_{xz} = 0.00000000

L_{yx} = -0.00000030 L_{yy} = 0.00001053 L_{yz} = 0.00000000

L_{zx} = 0.00000000 L_{zy} = 0.00000000 L_{zz} = 0.00011811

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.00014063 I_{xy} = -0.00000019 I_{xz} = 0.00000000

I_{yx} = -0.00000019 **I_{yy} = 0.00001053** I_{yz} = 0.00000001

I_{zx} = 0.00000000 I_{zy} = 0.00000001 I_{zz} = 0.00014050

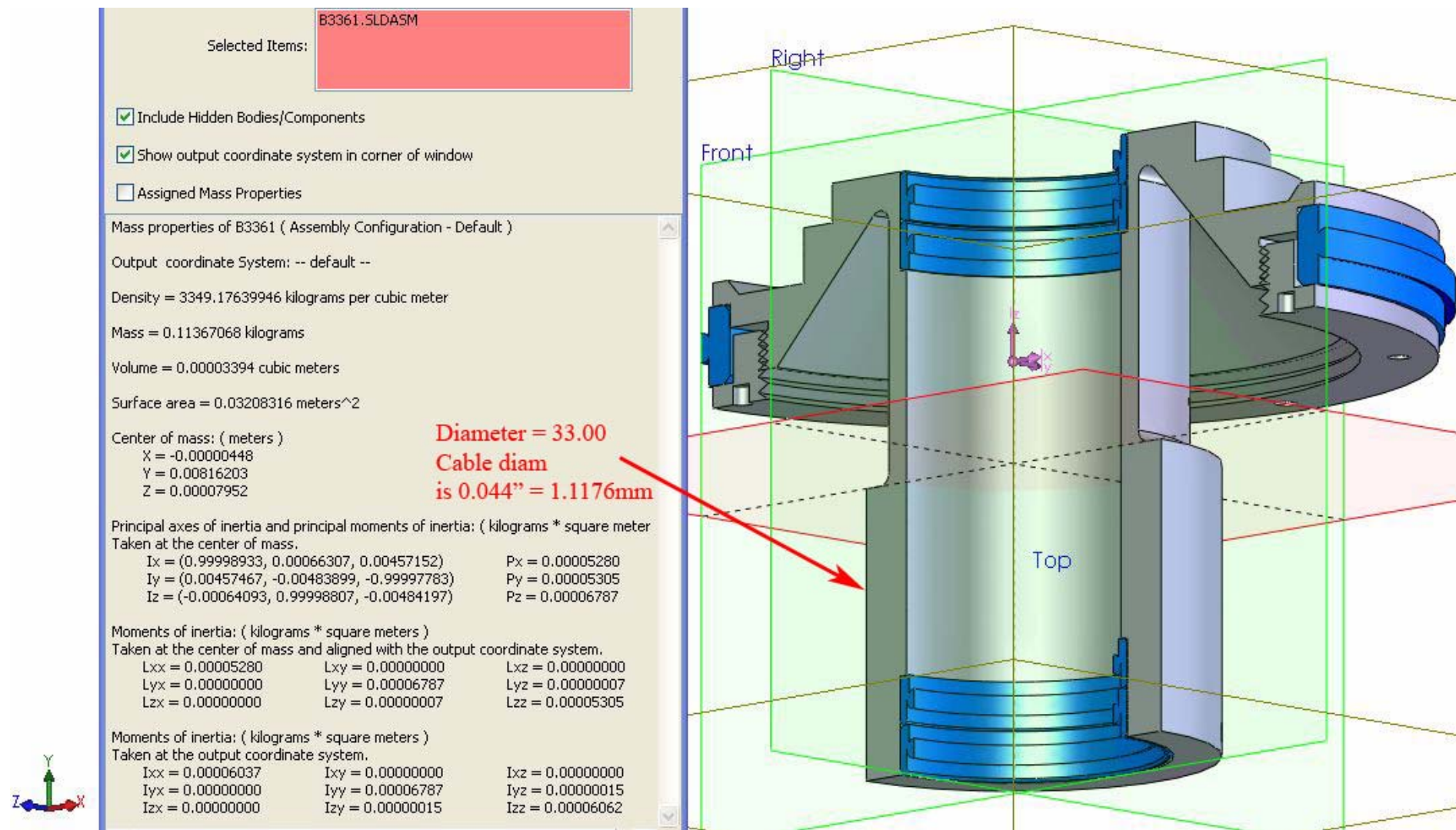


Figure 22 -- Wrist differential inner input-pulley pair driven by Motor 6.

Table 20 -- Mass properties of B3361 (Assembly Configuration - Default)

Density = 3349.17639946 kilograms per cubic meter

Mass = 0.11367068 kilograms

Volume = 0.00003394 cubic meters

Surface area = 0.03208316 meters²

Center of mass: (meters)

X = -0.00000448

Y = 0.00816203

Z = 0.00007952

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.99998933, 0.00066307, 0.00457152)$ $P_x = 0.00005280$

$I_y = (0.00457467, -0.00483899, -0.99997783)$ $P_y = 0.00005305$

$I_z = (-0.00064093, 0.99998807, -0.00484197)$ $P_z = 0.00006787$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00005280$ $L_{xy} = 0.00000000$ $L_{xz} = 0.00000000$

$L_{yx} = 0.00000000$ $L_{yy} = 0.00006787$ $L_{yz} = 0.00000007$

$L_{zx} = 0.00000000$ $L_{zy} = 0.00000007$ $L_{zz} = 0.00005305$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00006037$ $I_{xy} = 0.00000000$ $I_{xz} = 0.00000000$

$I_{yx} = 0.00000000$ **$I_{yy} = 0.00006787$** $I_{yz} = 0.00000015$

$I_{zx} = 0.00000000$ $I_{zy} = 0.00000015$ $I_{zz} = 0.00006062$

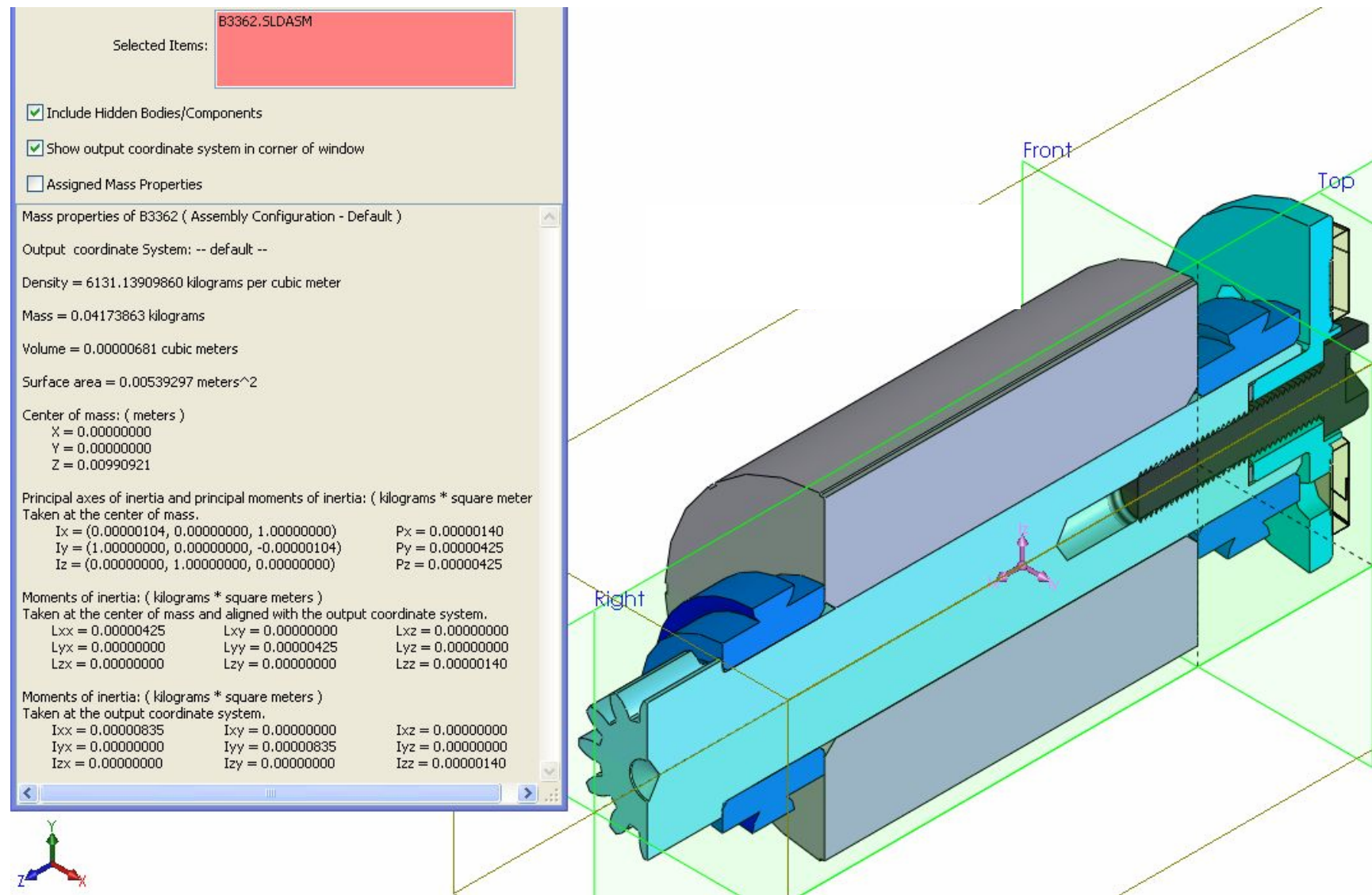


Figure 23 -- Motor-7 Inertia.

Table 21 --Mass properties of B3362 (Assembly Configuration - Default)

Density = 6131.13909860 kilograms per cubic meter

Mass = 0.04173863 kilograms

Volume = 0.00000681 cubic meters

Surface area = 0.00539297 meters²

Center of mass: (meters)

X = 0.00000000

Y = 0.00000000

Z = 0.00990921

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$I_x = (0.00000104, 0.00000000, 1.00000000)$ $P_x = 0.00000140$

$I_y = (1.00000000, 0.00000000, -0.00000104)$ $P_y = 0.00000425$

$I_z = (0.00000000, 1.00000000, 0.00000000)$ $P_z = 0.00000425$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$L_{xx} = 0.00000425$ $L_{xy} = 0.00000000$ $L_{xz} = 0.00000000$

$L_{yx} = 0.00000000$ $L_{yy} = 0.00000425$ $L_{yz} = 0.00000000$

$L_{zx} = 0.00000000$ $L_{zy} = 0.00000000$ $L_{zz} = 0.00000140$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$I_{xx} = 0.00000835$ $I_{xy} = 0.00000000$ $I_{xz} = 0.00000000$

$I_{yx} = 0.00000000$ $I_{yy} = 0.00000835$ $I_{yz} = 0.00000000$

$I_{zx} = 0.00000000$ $I_{zy} = 0.00000000$ **$I_{zz} = 0.00000140$**

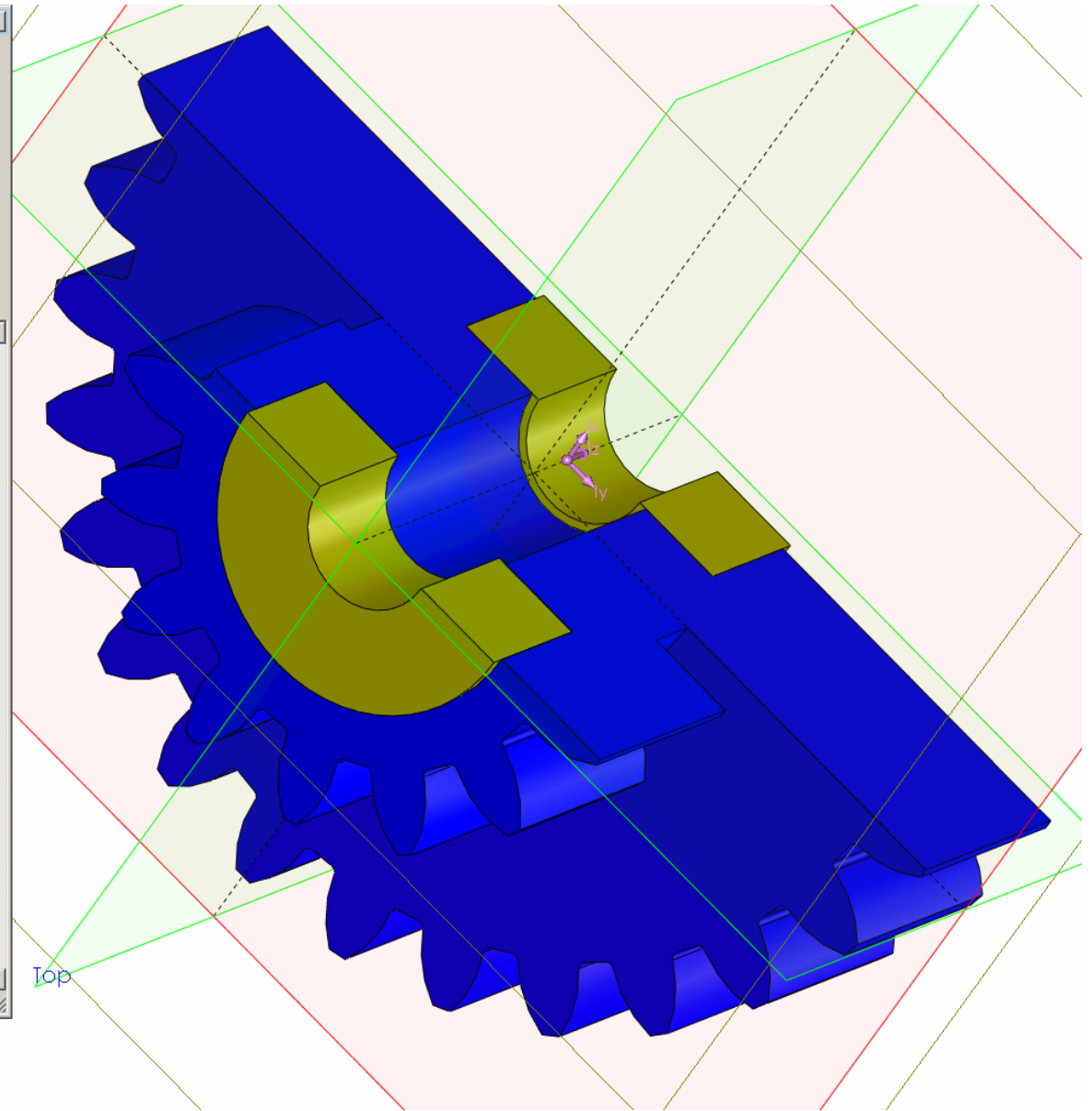
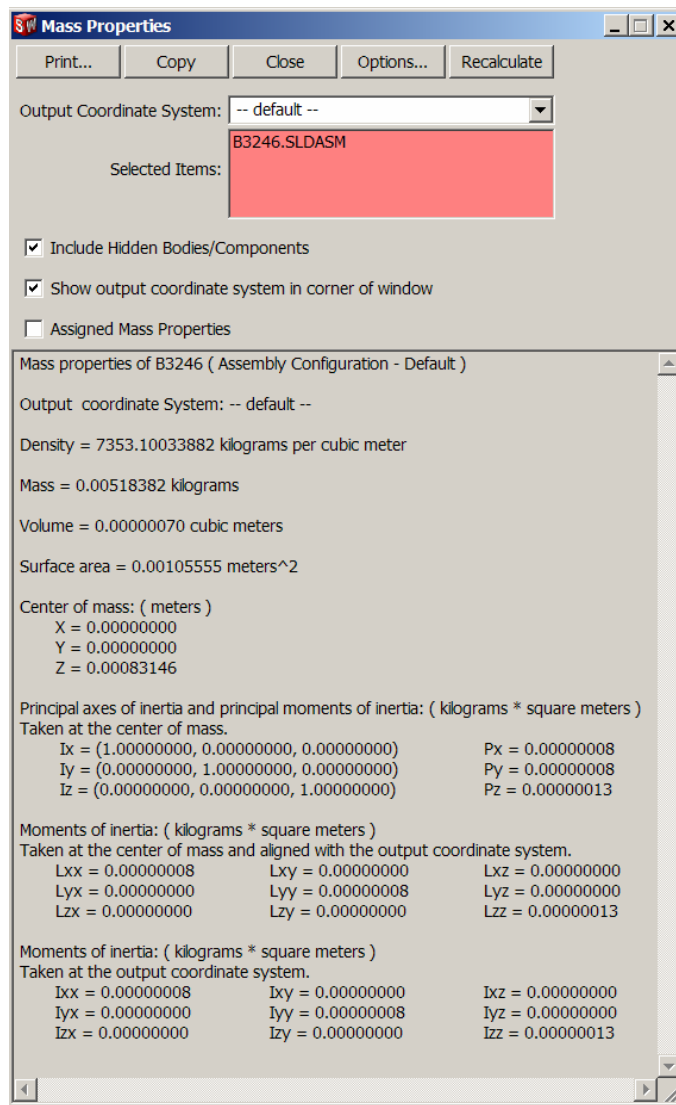


Figure 24 -- Geared 28/15 reducer.

Table 22 --Mass properties of B3246 (Assembly Configuration - Default)

Density = 7353.10033882 kilograms per cubic meter

Mass = 0.00518382 kilograms

Volume = 0.00000070 cubic meters

Surface area = 0.00105555 meters²

Center of mass: (meters)

X = 0.00000000

Y = 0.00000000

Z = 0.00083146

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (1.00000000, 0.00000000, 0.00000000) P_x = 0.00000008

I_y = (0.00000000, 1.00000000, 0.00000000) P_y = 0.00000008

I_z = (0.00000000, 0.00000000, 1.00000000) P_z = 0.00000013

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.00000008 L_{xy} = 0.00000000 L_{xz} = 0.00000000

L_{yx} = 0.00000000 L_{yy} = 0.00000008 L_{yz} = 0.00000000

L_{zx} = 0.00000000 L_{zy} = 0.00000000 L_{zz} = 0.00000013

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.00000008 I_{xy} = 0.00000000 I_{xz} = 0.00000000

I_{yx} = 0.00000000 I_{yy} = 0.00000008 I_{yz} = 0.00000000

I_{zx} = 0.00000000 I_{zy} = 0.00000000 **I_{zz} = 0.00000013**

Table 23 -- Geometric drive data and transmission ratios.

	SAVA PN	in	CabDia	Radius Definitions	BT PN	Radii	Dia	AdjDia	Radius	Ratios		
			mm				mm	mm	mm			
M1	SN2047	0.044	1.1176	Pinion of Motor Rotor	B2072	r_m	16.88	18.00	9.00	N_s1	3.6670	
	SN2047	0.044	1.1176	Pulley of Grenade	B2198	R_pp	64.88	66.00	33.00			
	SN2054	0.054	1.3716	Pinion of Grenade	B2198	r_pp	20.63	22.00	11.00	N_s2	11.4538	
	SN2054	0.054	1.3716	BasePulley	B1898	R_base	250.63	252.00	126.00			
										N = N_s1 * N_s2	42.0013	M1
M2&3	SN2047	0.044	1.1176	Pinion of Motor Rotor	B2072	r_m	16.88	18.00	9.00	N_s1	3.6670	
	SN2047	0.044	1.1176	Pulley of Grenade	B2198	R_pp	64.88	66.00	33.00			
	SN2054	0.054	1.3716	Pinion of Grenade	B2198	r_pp	20.63	22.00	11.00	N_s2	7.7041	
	SN2054	0.054	1.3716	Pulley of Differential Inputs	B1910	R_diff	168.13	169.50	84.75			
										N = N_s1 * N_s2	28.2510	M1 & M2
M4	SN2047	0.044	1.1176	Pinion of Motor Rotor	B2072	r_m	16.88	18.00	9.00	N_s1	3.4448	
	SN2047	0.044	1.1176	Pulley of ElbowPulleyPinion	B2196	R_pp	60.88	62.00	31.00			
	SN2054	0.054	1.3716	Pinion of ElbowPulleyPinion	B2196	r_pp	18.53	19.90	9.95	N_s2	5.2258	
	SN2054	0.054	1.3716	ElbowOutputHalfPulleys	B2186/7	R_diff	102.63	104.00	52.00			
										N = N_s1 * N_s2	18.0016	M4
M5&6	SN2019	0.018	0.4572	Pinion of Motor Rotor	B3357	r_m	12.70	13.16	6.58	N_s1	2.6599	
	SN2019	0.018	0.4572	Pulley of Stage1-2 PP	B3358	R_pp12	34.54	35.00	17.50			
	SN2024	0.024	0.6096	Pinion of Stage1-2 PP	B3358	r_pp12	15.00	15.61	7.80	N_s2	1.9103	
	SN2024	0.024	0.6096	Pulley of Stage2-3 PP	B3359	R_pp23	29.21	29.82	14.91			
	SN2047	0.044	1.1176	Pinion of Stage2-3 PP	B3359	r_pp23	16.76	17.88	8.94	N_s3	1.9084	
	SN2047	0.044	1.1176	Pulley of Differential Inputs	B3360/1	R_diff	33.00	34.12	17.06			
										N = N_s1 * N_s2 * N_s3	9.6973	M5&6
M7	N/A			Pinion of Motor Rotor	B3362	r_m	12			N_s1	2.3333	
	N/A			Idler Gear	B3246	R_pp	28					
	N/A			Pinion of Idler Gear	B3246	r_pp	15			N_s2	6.4000	
	N/A			Output Gear	B3347	R_out	96					
											14.9333	M7

Table 24 – Inertia of discrete drive components translated to the equivalent inertias (reflected) at each rotor.

		BTech	part inertia	cbl masses	cbl radius	inertia w/cbls	stg1	stg2	stg3	inertia@rotor
		PN	kg-m ²	kg	m	kg-m ²				kg-m ²
m1234	rotor	B3363	0.00010064	0.011	0.009	0.00010242	1.00	1.00	1.00	0.00010242
m123	grenade-pp X2	B2237	0.00009183	0.013	0.011	0.00018681	3.67	1.00	1.00	0.00001389
m2/3	diff input	B2331	0.00338288	0.013	0.075	0.00352913	3.67	11.45	1.00	0.00000200
m4	elbow pp	B2284	0.00005105	0.008	0.010	0.00005263	3.44	1.00	1.00	0.00000444
m56	rotor	B3357	0.00001565	0.001	0.007	0.00001574	1.00	1.00	1.00	0.00001574
m56a	S12-pp	B3358	0.00000558	0.002	0.008	0.00000582	2.66	1.00	1.00	0.00000082
m56b	S23-pp	B3359	0.00000358	0.003	0.009	0.00000406	2.66	1.91	1.00	0.00000016
m5	diff input (outer)	B3360	0.00001053	0.003	0.018	0.00001247	2.66	1.91	1.91	0.00000013
m6	diff input (inner)	B3361	0.00006787	0.003	0.013	0.00006888	2.66	1.91	1.91	0.00000073
m7	rotor	B3362	0.00000140	0.000	0	0.00000140	1.00	1.00	1.00	0.00000140
m7i	rotor	B3246	0.00000013	0.000	0	0.00000013	2.33	1	1.00	0.00000002

Table 25 – Combined total drive inertias by motor number reported both at the motor rotor and at the drive output.

Drive Number	Summed Components from Previous Table	Inertia@Rotor	Drive Ratio	Inertia@Output
		kg-m ²		kg-m ²
M1	m1234 + m123	0.00011631	42.00	0.20518962
M2	m1234 + m123 + m2/3	0.00011831	28.25	0.09442836
M3	m1234 + m123 + m2/3	0.00011831	28.25	0.09442836
M4	m1234 + m4	0.00010686	18.00	0.03462804
M5	m56 + m56a + m56b + m5	0.00001685	9.70	0.00158448
M6	m56 + m56a + m56b + m6	0.00001745	9.70	0.00164089
M7	m7+m7i	0.00000142	14.93	0.00031753