Inertia Tensors, Masses, and CGs for the BarrettHand BH8-262

(version 02, 2008-Mar-04)

Dear Reader,

The initial draft of this document was prepared for Yuandong Yang <u>yuandong@robotics-mail.cs.umass.edu</u> in late August, 2007. Yuandong may have information on how he used the data and the results of its use. If you find any errors in this document, please feed them back to me, its author, Bill Townsend <u>wt@barrett.com</u>

The data was not updated between Versions 01 and 02. The only changes were a rewrite of this cover sheet and deleting a blank last page.

The data given was calculated from Barrett's SolidWorks CAD model using SolidWorks2006, version 5.1. (The reader may may find it interesting that the original BarrettHand was the first machine ever designed in SolidWorks CAD. Indeed the first manuals shipped with the initial launch of SolidWorks contained almost exclusively BarrettHand part, assembly, and drawing examples.)

While this document is rough around the edges, the graphics are clear, and I believe that the data matches the model within 1 percent. I exploited transparency properties as much as possible to make clear which parts are associated with which link. Since no one is likely to wish to attempt computed-torque control on the Hand axes (since the frictions in the Hand are very high), I did not compute the backdriven, reflected drive inertias of the drives. Since backdriven drive inertias have no effect on gravity terms, the frame inertias should give you good results for controlling the WAM arm and wrist torques as functions of hand-finger positions.

The base of the Hand is modeled without the separable ring nut, which is not used to connect the BarrettHand to the WAM arm.

When summed, the data from this document gives the strain-gaged Hand mass at 1.235 kg (B3470 + 2 * B3471 + 3 * (B3472 + B3476)) and the non-strain-gaged Hand mass at 1.223 kg (B3470 + 2 * B3471 + 3 * (B3473 + B3476)).

These numbers are slightly higher than the true weights of the Hand. We measured a Hand (ser#HND-132) without strain-gage beams installed, but with their connectors installed on 2008-Mar-04 which weighed in at 1.220 kg. The nominal spec for a Hand is 1.180 kg, and we are not sure of the source of the 40-gm difference.

To repeat, please let me know as you find (or even suspect) other errors in the data presented here.

Good luck,

Bill T. wt@barrett.com





Mass properties of B3470 (Assembly Configuration - WithStrainGageOption)

Density = 3205.70736898 kilograms per cubic meter

Mass = 0.63352875 kilograms

Volume = 0.00019763 cubic meters

Surface area = 0.23982378 meters²

Center of mass: (meters)

X = 0.00035500Y = -0.00499005Z = 0.04864979

Principal axes of inertia and principal moments of inertia: (kilograms * square meters) Taken at the center of mass.

Ix = (-0.03383328, -0.55260676, 0.83275511)	Px = 0.00059171
Iy = (0.00298160, -0.83328425, -0.55283675)	Py = 0.00090512
Iz = (0.99942304, -0.01622134, 0.02984039)	Pz = 0.00102153

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00102103	Lxy = 0.00000775	Lxz = -0.00001230
Lyx = 0.00000775	Lyy = 0.00080944	Lyz = -0.00014417
Lzx = -0.00001230	Lzy = -0.00014417	Lzz = 0.00068788

Moments of inertia: (kilograms * square meters)

Ixx = 0.00253625	Ixy = 0.00000662	Ixz = -0.00000136
Iyx = 0.00000662	Iyy = 0.00230896	Iyz = -0.00029797
Izx = -0.00000136	Izy = -0.00029797	Izz = 0.00070373





Mass properties of B3471 (Assembly Configuration - WithStrainGageOption)

Density = 3738.20010426 kilograms per cubic meter

Mass = 0.16252678 kilograms

Volume = 0.00004348 cubic meters

Surface area = 0.05418535 meters²

Center of mass: (meters)

X = 0.03201666Y = -0.00086502Z = -0.01569925

Principal axes of inertia and principal moments of inertia: (kilograms * square meters) Taken at the center of mass.

Ix = (0.97919668, -0.02501033, 0.20136621)	Px = 0.00002332
Iy = (0.20275694, 0.08163084, -0.97582069)	Py = 0.00008053
Iz = (0.00796790, 0.99634878, 0.08500366)	Pz = 0.00008827

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00002567	Lxy = -0.00000146	Lxz = 0.00001128
Lyx = -0.00000146	Lyy = 0.00008818	Lyz = -0.0000094
Lzx = 0.00001128	Lzy = -0.0000094	Lzz = 0.00007827

Moments of inertia: (kilograms * square meters)

Ixx = 0.00006585	Ixy = -0.00000596	Ixz = -0.00007042
Iyx = -0.00000596	Iyy = 0.00029484	Iyz = 0.00000126
Izx = -0.00007042	Izy = 0.00000126	Izz = 0.00024499

Mass Properties	Front		
Print Copy Close Options Recalculate			
Output Coordinate System: default			
B3472.SLDASM			
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Show output coordinate system in corner of window			
Assigned Mass Properties			
Mass properties of B3472 (Assembly Configuration - Default)			
Output coordinate System: default		52	
Density = 0.003 grams per cubic millimeter		RA I	
Mass = 57.957 grams			\sim
Volume = 19754.166 cubic millimeters			
Surface area = 26796.433 millimeters^2			
Center of mass: (millimeters)	Right		/
X = 31.720 Y = 1.070			
Z = -0.586			
Principal axes of inertia and principal moments of inertia: (grams * square millimeters)		(3)	
Taken at the center of mass. $T_x = (0.999, 0.011, 0.051)$			All a
IX = (0.535, 0.011, 0.031)			AN
Iz = (-0.051, -0.029, 0.998) Pz = 36913.699	294		
Moments of inertia: (grams * square millimeters)	7600		
Lxx = 4614.085 Lxy = 337.086 Lxz = 1649.347			
Lyx = 337.086 Lyy = 35902.138 Lyz = 46.158			
L2X = 1649.347 L2Y = 46.158 L2Z = 36828.645			
Moments of inertia: (grams * square millimeters) Taken at the output coordinate system			
Ixx = 4700.415 Ixy = 2304.981 Ixz = 571.511			
Iyx = 2304.981 Iyy = 94237.082 Iyz = 9.785 Izx = 571.511 Izy = 9.785 Izz = 95210.076			
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Mass properties of B3472 (Assembly Configuration - Default)

Density = 3085.63509216 kilograms per cubic meter

Mass = 0.05795741 kilograms

Volume = 0.00001878 cubic meters

Surface area = 0.02509034 meters^2

Center of mass: (meters)

X = 0.03172018Y = 0.00107042Z = -0.00058628

Principal axes of inertia and principal moments of inertia: (kilograms * square meters) Taken at the center of mass.

Ix = (0.99863993, 0.01080386, 0.05100547)	Px = 0.00000453
Iy = (-0.01224756, 0.99953071, 0.02807762)	Py = 0.00003590
Iz = (-0.05067819, -0.02866412, 0.99830361)	Pz = 0.00003691

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00000461	Lxy = 0.00000034	Lxz = 0.00000165
Lyx = 0.00000034	Lyy = 0.00003590	Lyz = 0.00000005
Lzx = 0.00000165	Lzy = 0.00000005	Lzz = 0.00003683

Moments of inertia: (kilograms * square meters)

Ixx = 0.00000470	Ixy = 0.00000230	Ixz = 0.00000057
Iyx = 0.00000230	Iyy = 0.00009424	Iyz = 0.00000000
Izx = 0.00000057	Izy = 0.00000000	Izz = 0.00009521

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Print Copy Close Options Recalculate	
Output Coordinate System: default	
B3473.SLDASM	
Selected Items:	
	Тор
✓ Include Hidden Bodies/Components	
Show output coordinate system in corner of window	
Assigned Mass Properties	
Mass properties of B3473 (Assembly Configuration - Default)	
Output coordinate System: default	
Density = 2925.73632911 kilograms per cubic meter	
Mass = 0.05380765 kilograms	
Volume = 0.00001839 cubic meters	
Surface area = 0.02407868 meters^2	
Center of mass: (meters) X = 0.03122559 Y = 0.00112180 Z = -0.00062961	Bight
$ \begin{array}{l} \label{eq:principal axes of inertia and principal moments of inertia: (kilograms * square meters) \\ \end{tabular} Taken at the center of mass. \\ \end{tabular} Ix = (0.99854419, 0.01259932, 0.05244770) \\ \end{tabular} Px = 0.00000446 \\ \end{tabular} Iy = (-0.01405156, 0.99952542, 0.02741326) \\ \end{tabular} Py = 0.00003523 \\ \end{tabular} Iz = (-0.05207742, -0.02811033, 0.99824734) \\ \end{tabular} Pz = 0.00003625 \\ \end{array}$	AIS A
Moments of inertia: (kilograms * square meters) Taken at the center of mass and aligned with the output coordinate system. Lxx = 0.00000455 Lxy = 0.00000039 Lyx = 0.00000039 Lyy = 0.00003522 Lxx = 0.000000166 Lzy = 0.0000005 Lzx = 0.00000166 Lzy = 0.0000005	
Moments of inertia: (kilograms * square meters) Taken at the output coordinate system. Ixx = 0.00000464 Ixy = 0.00000227 Ixz = 0.00000061	
Iyx = 0.00000227 Iyy = 0.00008771 Iyz = 0.0000001 Izx = 0.00000061 Izy = 0.00000001 Izz = 0.00008869	
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Mass properties of B3473 (Assembly Configuration - Default)

Density = 3088.85010288 kilograms per cubic meter

Mass = 0.05380764 kilograms

Volume = 0.00001742 cubic meters

Surface area = 0.02237259 meters^2

Center of mass: (meters)

$$\begin{split} X &= 0.03122559 \\ Y &= 0.00112179 \\ Z &= -0.00062961 \end{split}$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters) Taken at the center of mass.

Ix = (0.99854419, 0.01259930, 0.05244767)	Px = 0.00000446
Iy = (-0.01405150, 0.99952544, 0.02741244)	Py = 0.00003523
Iz = (-0.05207740, -0.02810950, 0.99824736)	Pz = 0.00003625

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00000455	Lxy = 0.00000039	Lxz = 0.00000166
Lyx = 0.00000039	Lyy = 0.00003522	Lyz = 0.00000005
Lzx = 0.00000166	Lzy = 0.00000005	Lzz = 0.00003616

Moments of inertia: (kilograms * square meters)

Ixx = 0.00000464	Ixy = 0.00000227	Ixz = 0.00000061
Iyx = 0.00000227	Iyy = 0.00008771	Iyz = 0.00000001
Izx = 0.00000061	Izy = 0.00000001	Izz = 0.00008869



Mass properties of B3474 (Assembly Configuration - Default)

Density = 2245.68077726 kilograms per cubic meter

Mass = 0.01610049 kilograms

Volume = 0.00000717 cubic meters

Surface area = 0.00949114 meters²

Center of mass: (meters)

X = 0.00459747Y = -0.00019176Z = 0.00041465

Principal axes of inertia and principal moments of inertia: (kilograms * square meters) Taken at the center of mass.

Ix = (0.50695587, -0.06237633, 0.85971212)	Px = 0.00000115
Iy = (0.85340706, -0.10393084, -0.51077859)	Py = 0.00000122
Iz = (0.12121110, 0.99262660, 0.00054405)	Pz = 0.00000163

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00000121	Lxy = -0.00000005	Lxz = 0.00000003
Lyx = -0.00000005	Lyy = 0.00000163	Lyz = 0.00000000
Lzx = 0.00000003	Lzy = 0.00000000	Lzz = 0.00000117

Moments of inertia: (kilograms * square meters)

Ixx = 0.00000122	Ixy = -0.00000007	Ixz = 0.00000006
Iyx = -0.00000007	Iyy = 0.00000197	Iyz = 0.00000000
Izx = 0.00000006	Izy = 0.00000000	Izz = 0.00000151



Mass properties of B3475 (Assembly Configuration - Default)

Density = 2378.27997141 kilograms per cubic meter

Mass = 0.01811732 kilograms

Volume = 0.00000762 cubic meters

Surface area = 0.00730548 meters²

Center of mass: (meters)

X = 0.03313970Y = 0.00360812Z = 0.00000000

Principal axes of inertia and principal moments of inertia: (kilograms * square meters) Taken at the center of mass.

Ix = (0.99992500, 0.01224728, 0.00000000)	Px = 0.00000154
Iy = (0.00000000, 0.00000128, -1.00000000)	Py = 0.00000390
Iz = (-0.01224728, 0.99992500, 0.00000129)	Pz = 0.00000471

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00000154	Lxy = 0.00000004	Lxz = 0.00000000
Lyx = 0.00000004	Lyy = 0.00000471	Lyz = 0.00000000
Lzx = 0.00000000	Lzy = 0.00000000	Lzz = 0.00000390

Moments of inertia: (kilograms * square meters)

Ixx = 0.00000177	Ixy = 0.00000221	Ixz = 0.00000000
Iyx = 0.00000221	Iyy = 0.00002461	Iyz = 0.00000000
Izx = 0.00000000	Izy = 0.00000000	Izz = 0.00002403



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Mass properties of B3476 (Assembly Configuration - Default)

Density = 2493.18839434 kilograms per cubic meter

Mass = 0.03421781 kilograms

Volume = 0.00001372 cubic meters

Surface area = 0.01467305 meters²

Center of mass: (meters)

X = 0.01970974Y = 0.00182016Z = 0.00020041

Principal axes of inertia and principal moments of inertia: (kilograms * square meters) Taken at the center of mass.

Ix = (0.99621484, 0.08661050, -0.00739050)	Px = 0.00000279
Iy = (-0.00815345, 0.00845851, -0.99993099)	Py = 0.00001214
Iz = (-0.08654201, 0.99620634, 0.00913267)	Pz = 0.00001336

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00000287	Lxy = 0.0000091	Lxz = -0.00000007
Lyx = 0.00000091	Lyy = 0.00001329	Lyz = -0.0000002
Lzx = -0.00000007	Lzy = -0.0000002	Lzz = 0.00001214

Moments of inertia: (kilograms * square meters)

Ixx = 0.00000299	Ixy = 0.00000214	Ixz = 0.00000007
Iyx = 0.00000214	Iyy = 0.00002658	Iyz = 0.00000000
Izx = 0.00000007	Izy = 0.00000000	Izz = 0.00002555